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# Do the Students Experience Difficulties in Mathematical Connections to Solve Mathematical Problems? 

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#### Abstract

The main purpose of studying mathematics is that students can solve problems, both mathematical problems and real-life problems. In this way, mathematical connections play an important role to enable students to solve mathematical problems. Students' difficulties in mathematical connections can cause difficulties in solving problems. This study aims to describe the difficulties experienced by students in solving mathematical problems. This study is qualitative in nature with a phenomenological approach. Data were collected by using mathematical connection tests and interviews after the test. The participants of this study were 31 high school students from five schools in Yogyakarta Special Region and Central Java Province, Indonesia. Data analysis began with a quantitative description of students' difficulties related to the ability of mathematical connections followed by qualitative analysis of interview results. The findings showed that most students experienced difficulties in making mathematical connections such as in different representation, part-whole relationships, connections between mathematical concepts, and interrelationships between mathematical procedures. Several causes of such difficulties and further actions were also discussed in this study.


Keywords: mathematical connections, problem solving, student difficulties

## 1. Introduction

Mathematics is a compulsory subject learnt from primary to tertiary education. This subject plays an important role in the advancement and development of science and technology, and also contributes directly to human survival. In addition, mathematics is not just arithmetic, but it can also be used to practice a variety of thinking skills, such as critical thinking (Appelbaum, 2000; Lince, 2016; Suh \& Seshaiyer, 2013), creative thinking (Leikin \& Pitta-Pantazi, 2013; Lince, 2016), logical thinking (Hodge, 2003; Lince, 2016), and higher order thinking skills (Apino \& Retnawati, 2017, 2019). The importance of mathematics encourages many countries to keep creating innovations in strategies and approaches to learning mathematics in order to make mathematics more understandable and applicable in real-life situations.

One of the keys in learning mathematics is problem solving (NCTM, 2000). Problem solving is in line with the spirit of mathematics as a means to develop thinking skills. In the context of mathematics education, this problem solving is used to introduce and familiarize students with how to understand a phenomenon related to mathematical concepts and things related to the application of mathematics in everyday life. By using problem solving, the students are then expected to be able to plan and find solutions to various problems systematically and logically. This ability is fundamentally important as it can help the students face increasingly complex challenges in life.

A number of literatures categorize problem solving as one of the competencies that must be possessed for success in the 21st century besides critical thinking, creativity, collaboration and communication (Partnership for 21st Century Learning, 2019). Today, problem solving is no longer seen as a written skill, but from a broader perspective, it evolves into a basic skill used to compete in the world of work and even to answer the challenges of this era. In order to reach this skill, other abilities are needed. As formulated by NCTM (2000), in mathematics learning standards, another ability such as mathematical connection must be practiced by students in addition to problem solving. NCTM (2000) highlights that mathematical connection is a tool for problem solving. Mathematical connections help students recognize and use relationships between mathematical ideas and use them in different contexts (Dolores-Flores et al., 2018). Having strong mathematical connections will also enhance mathematical understanding (García-García \& Dolores-Flores, 2017; Kenedi et al., 2019; Silver et al., 2009) and student achievement (Kartikasari \& Widjajanti, 2017; Ndiung \& Nendi, 2018).

Mathematical connections are generally associated with three things, namely connections related to the application of mathematics to real-life contexts (Blum et al., 2007; Monroe \& Mikovch, 1994; Mwakapenda, 2008), mathematical connections with other disciplines (Blum et al., 2007; Mwakapenda, 2008) and connections between mathematical ideas or concepts themselves (Blum et al., 2007; Monroe \& Mikovch, 1994; Mwakapenda, 2008). Businskas (2008) suggests that most literature only focus on examining the connection between mathematics and real-world situations without exploring how interconnection in mathematics itself. The mathematical connections in Calculus material are still few in number (García-García \& Dolores-Flores, 2017). In fact, the ability to make connections between mathematics itself is very important for understanding mathematical concepts (Anthony \& Walshaw, 2009), and for their application to other scientific disciplines (Mhlolo et al., 2012). Thus, interconnection in mathematics becomes an interesting topic to discuss.

In general, interconnection in mathematics can be defined as a relation between ideas or processes that can be used to link topics in mathematics; a process of making or recognizing the relationships between mathematical ideas; an association made by an individual between two or more mathematical ideas; a causal or logical relationship or interdependence between two mathematical entities (Businskas, 2008). Making connections between mathematical ideas is an important indicator of understanding (Berry \& Nyman, 2003), but at the same time, students who have had some understanding will also be able to make connections between ideas, concepts,
procedures, representations, and meanings (García-García \& Dolores-Flores, 2017). In this way, the ability to make interconnections in mathematics can be considered as an indicator of deep understanding, and vice versa.

In this study, mathematical connection is focused on interconnection in mathematics itself. Businskas (2008) suggests a framework for thinking about mathematical connections in practice. The framework of thinking can be operationally used as an indicator of mathematical connections consisting of five categories. The categories include different representation (DR) as a form of mathematical connections, part-whole relationships (PWR), connections where A implies B (IM), connections showing that A is a procedure for doing $B$ (PD), and instructional oriented connection (IOC) that show how certain concepts are pre-requisites for understanding related concepts. GarcíaGarcía and Dolores-Flores (2017) explores the intra-mathematical connections made by high school students when they solved Calculus tasks. The results show that they found several types of connection mathematics in solving Calculus tasks including the following: different representations, procedural, features, reversibility and meaning as a connection. Through these indicators, mathematical connections can be identified more easily and the extent to which mathematical connections can be easily measured.

Some other studies also report that the students' mathematical connection abilities in various levels need serious attention. Lapp et al. (2010) report that undergraduate students encountered difficulties in making connections between various concepts, such as the connection between eigenvalues and eigenvectors in algebra learning. DoloresFlores et al. (2018) conducted research to explore the mathematical connections of preuniversity students while solving tasks involving the rates of change and the result showed that the students only made mathematical connections of procedural types while other types of mathematical connections such as the common features and the generalization were scarcely made by the students. Siregar and Surya (2017) analyzed the junior high school students' abilities in mathematical connections using tests of mathematical connections and the result showed that their abilities were still low. Similarly, Kenedi et al. (2019) investigated the elementary school students' mathematical connection ability in solving mathematics problems and the result showed that their abilities were also low. The results of these studies can be used as a basis for improving the quality of mathematics learning that is oriented towards improving mathematical connections.

In practice, several studies report a number of obstacles in teaching mathematical connections. Dolores-Flores et al. (2018) reported that lack of conceptual understanding and difficulties in manipulating algebra were the main obstacles in making mathematical connections. Arjudin et al. (2016) also reported that students' difficulties in making mathematical connections were caused by errors in connecting with conceptual knowledge and procedural knowledge. Lack of familiarity with the mathematical connection problems also becomes another obstacle for students in developing their mathematical connection ability. In this way, Agustini et al. (2017) suggest familiarizing students with mathematical connection problems by using openended problems.

To deal with a variety of students' difficulties related to mathematical connections, a number of remedial efforts need to be made. The starting point for improvement can be done by identifying students' difficulties in solving problems that measure students' mathematical connections. Dolores-Flores et al. (2018) point out that mathematical connections occur when students carry out specific tasks and therefore can be identified from the writings or arguments produced by the students. Related to the urgency of the mathematical connection ability, this study aims to describe the difficulties experienced by the students in solving mathematical problems. By identifying the difficulties, educators can seek improvement and also design learning models to overcome the problems.

## 2. Methods

### 2.1. Type of Study

This study was classified as phenomenology, a type of qualitative research methods. The phenomenon was about the students' difficulty in making mathematical connections, especially in solving mathematical problems. One common phenomenon which occurred when students solved mathematical problems was that students already knew a concept, but they had difficulty in connecting the concept with other mathematical concepts. This phenomenon often gave negative impact on their understanding of mathematical concepts and their academic achievement in learning mathematics.

### 2.2. Research Participants

The participants of this study were 31 high school students from five schools in Yogyakarta Special Region and Central Java Province, Indonesia. The schools were selected as representatives with high, medium, and low academic achievement. The students involved in this study were between 15 and 17 years old when the study was conducted.

### 2.3. Data Collection

The data were collected through tests and interviews. The test consisted of mathematical problems (items) containing concepts that had been taught at schools. It comprised of three items and each of them required mathematical connection ability to solve it. These items were taken from the questions in college entrance exam in Indonesia that had been released and re-validated. The validity of the test instrument was proven through content validation by asking an expert to agree on the suitability of the item with the indicator. The indicators of mathematical connection abilities used in this study included different representation (DR), part-whole relationships (PWR), connections where A implies B (IM), and connections showing that A is a procedure for doing B (PD). Item 1 was used to measure the students' mathematical connection ability to solve the problem of a two-variable linear equation (see Figure 2). Item 2 was used to measure the students' mathematical connection ability to solve the problem of a trigonometric equation (see Figure 3). Item 3 was used to measure the students' mathematical connection ability to solve the problem of a circle (see Figure 4).

Interviews with the students were conducted after they finished the test. The interviews aimed to know the students' perceptions of the problems being tested. In this case, the students were asked to show which difficult parts of the problem-solving process they found. The interviews were also focused on finding obstacles or causes of the difficulties encountered by the students in solving mathematical connection problems. Prior to the study, the students were informed that the tests and interviews conducted during the data collection would not affect their academic achievement at school.

### 2.4. Data Analysis

The collected data were then analyzed quantitatively and qualitatively. The quantitative analysis was done by calculating the percentage of the students' difficulties for each item and indicator. Meanwhile, the qualitative analysis was done by examining the students' answers and mapping the errors. The results of the interviews were also qualitatively analyzed using an analytical technique developed by Bogdan and Biklen (1982) by analyzing the relationships between themes from the qualitative data obtained from the interviews.

## 3. Results

### 3.1. Description of Difficulties in Students' Mathematical Connection Ability

In this study, the students' mathematical connection ability is seen through four main indicators, namely different representation (DR), part-whole relationships (PWR), connections where A implies B (IM), and connections showing that A is a procedure for doing $B$ (PD). The ability of the students to master each of the mathematical connection indicators is categorized into three levels of mastery including the following: "High Mastery," "Average Mastery," and "Low Mastery." The "Average Mastery" and "Low Mastery" levels are used as a basis for identifying students who experience mathematical connection difficulties. In other words, when the mastery of each indicator only reaches the level of "Average Mastery" and "Low Mastery," the students were then categorized as experiencing mathematical connection difficulties. The percentage of students who experience mathematical connection difficulties and the level of student mastery of each indicator in each question are presented in Table 1.

Table 1 shows that the percentage of students who have high mastery in each indicator tested for each question was under $50 \%$. In general, this number shows that most students still experienced difficulty for each indicator of mathematical connection ability. For Problem 1, Connections where A Implies B (IM) was perceived by the students as the most difficult indicator, where $73.68 \%$ of the students experienced difficulty in this indicator. For Problem 2, however, the most difficult indicator perceived by the students was connection showing that A is a procedure for doing B (PD), where $73.68 \%$ of students experienced difficulty in this indicator. For Problem 4, when compared to Problem 1 and Problem 2, the percentage of student difficulties for each indicator of mathematical connection ability was much higher. Of the four mathematical connection indicators tested in Problem 4, more than $80 \%$ of the students had difficulty and even $97.37 \%$ of the students had difficulty in the part-whole relationships (PWR) indicator. For the PWR indicator in particular, Problem 1 and Problem 2 have not accommodated this indicator, and therefore, the students' difficulty
for this indicator in Problem 3 could not be compared. The fact that the PWR indicator reached the highest percentage showed that the students experienced great difficulty in constructing answers using this indicator. Overall, it can be concluded that the students' mathematical connection difficulties occur in all indicators where PWR is the most difficult indicator and PD is the second most difficult indicator for the students. The comparison between the students who had mastered and those who faced difficulties of mathematical connection can be seen in Figure 1.

Table 1. Percentage of Students Experiencing Mathematical Connection

| Indicators of mathematical connection | High <br> Mastery |  | Average Mastery |  | Low Mastery |  | Difficul- <br> ties ${ }^{1)}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $n$ | \% | $n$ | \% | $n$ | \% | $n$ | \% |
| Problem 1: |  |  |  |  |  |  |  |  |
| Different Representation (DR) | 16 | 42.11 | 7 | 18.42 | 15 | 39.47 | 22 | 57.89 |
| Part-Whole Relationships (PWR) | - 2) | - | - | - | - | - | - | - |
| Connections where A Implies B (IM) | 10 | 26.32 | - | - | 28 | 73.68 | 28 | 73.68 |
| Connections that show that A is a procedure for doing B (PD) | 17 | 44.74 | 6 | 15.79 | 15 | 39.47 | 21 | 55.26 |
| Problem 2: |  |  |  |  |  |  |  |  |
| Different Representation (DR) | 18 | 47.37 | 10 | 26.32 | 10 | 26.32 | 20 | 52.63 |
| Part-Whole Relationships (PWR) | ${ }^{-2)}$ | - | - | - | - | - | - | - |
| Connections where A Implies B (IM) | 18 | 47.37 | - | - | 20 | 52.63 | 20 | 52.63 |
| Connections that show that A is a procedure for doing B (PD) | 10 | 26.32 | 9 | 23.68 | 19 | 50.00 | 28 | 73.68 |
| Problem 3: |  |  |  |  |  |  |  |  |
| Different Representation (DR) | 5 | 13.16 | - | - | 33 | 86.84 | 33 | 86.84 |
| Part-Whole Relationships (PWR) | 1 | 2.63 | 15 | 39.47 | 22 | 57.89 | 37 | 97.37 |
| Connections where A Implies B (IM) | 7 | 18.42 | - | - | 31 | 81.58 | 31 | 81.58 |
| Connections that show that A is a procedure for doing B (PD) | 2 | 5.26 | 13 | 34.21 | 23 | 60.53 | 36 | 94.74 |

## Notes:

${ }^{1)}$ Difficulties in mathematical connection is the total number of students who have average and low mastery in each indicator.
${ }^{2}$ ) Indicator is not tested in the item.
$n$ is the number of students.
Figure 1 shows that the gap between students who had mastered the indicators and those who had not mastered the indicators was too big, especially in Problem 3. From Figure 1 it can be seen that the number of students who have not mastered the indicators is bigger than those who have mastered the indicators of mathematical connection. Meanwhile, the gap for DR, PWR, PD indicators in all problems (Problem 1, Problem 2, and Problem 3) looked different. Thus, it can be concluded that for each mathematical connection indicator in each given problem, the number of students who experienced difficulty is higher than those who did not experience it.


Figure 1. The comparison between the students who had mastered and those who faced difficulties of mathematical connection

Qualitative data were also collected to confirm the findings. Based on the results of qualitative data reduction from students' written comments and interviews, a number of difficulties faced by the students in solving mathematical connection problems are presented in Table 2.

Table 2. Identification of Student Difficulty in Solving Mathematical Connection Problems

| Identification of Student Difficulty | Conclusion |
| :--- | :--- |
| The students were unfamiliar with mathematical <br> connection problems. <br> The students had difficulty in reading mathematical <br> patterns. <br> The students had difficulty in connecting mathematical <br> concepts. <br> The students had difficulty in mathematic manipulation. | The students were not <br> well trained to solve <br> mathematical <br> connection problems <br> because of lack of <br> familiarity. |
| The students did not understand several terms in the <br> problems. <br> The students had difficulty in understanding the <br> problems completely. <br> The students found it hard to identify important points <br> from the problems. <br> The students forgot mathematical formulas. | The students lacked of <br> conceptual understan- <br> ding. |
| The problems included too long words. | The students were not <br> interested in word <br> problems. |
| The problems required repeated reading. |  |

Based on Table 2, it can be seen that there are three main causes of students' difficulty in solving the mathematical connection problems. The first is lack of familiarity with mathematical connection problems as seen in the following excerpts of student interviews.
"... I've never worked on a problem about fractions like in Problem 1." (Student 3)
"... I've never met a problem about a circle with another circle. A problem about a circle usually asks for tangents only. That's not about a circle intersecting another circle. The problem is difficult and unfamiliar to me." (Student 1)

The student interviews showed that so far, the students were only used to working on routine problems. Thus, they faced difficulty when doing non-routine problems, such as mathematical connection. In addition, they had difficulty in reading mathematical patterns as expressed by two students in the following interview excerpts.
"... if we can find the pattern, the trigonometric identity is actually easy, but it's difficult for me to find the pattern because I don't have good sense to do that." (Student 12)
"... I have difficulty seeing the pattern because of its fraction, and in my opinion, solving linear equation in this problem is very difficult." (Student 10)

The difficulty of linking between concepts and manipulating mathematical operations caused the students to fail in their attempt to determine the next procedure for solving the problem, as illustrated in the following interview excerpts.
"... the problem is not too confusing, but I just don't really understand the trigonometric identity and quadratic equation, then I find it hard to associate them." (Student 5)
"... I stopped at A and B because I didn't find a comparison to calculate the value of $A$ and
B." (Student 12)

Lack of conceptual understanding is one of the causes of the students' difficulty in solving mathematical connection problems as stated by the students in the following excerpts.
"... I've difficulty in this problem, I don't understand the meaning of 'radius' and also the problem in general. So, I have no idea for what the problem means." (Student 2)
"... I'm having a hard time understanding the problem, applying the trigonometric identity is quite difficult me." (Student 10)
"... I don't really understand about calculating the area of a circle, and I find it hard to separate the parts of the circle." (Student 5)

The student interviews proved that the students were still weak in the basic concepts of mathematics. In this case, they did not know the term 'radius' and how to calculate the area of a circle. Their low comprehension of such basic concepts caused them to have difficulty in understanding the purpose of the problem, and therefore, they failed to plan the correct procedure for solving the problem.

One of the common challenges faced by the students in problem solving activities was that they were lazy to read word problems. This is illustrated by the following excerpts.
> "... the word problem consisted of long sentences that demanded a lot of concentration on understanding the points. Well, I can understand the points. So, I separated the points first and then calculated the area." (Student 9)
> "... what was asked in the problem was actually quite simple, but the description was not straightforward." (Student 11)

It appeared that the students did not really enjoy reading the context or rather long information. This condition led to difficulty in understanding the problem as a whole and also planning mathematical procedures used to solve the problem. As a result, the students' progress in problem solving related to mathematical connections would be hindered. To illustrate the various difficulties students, have in solving mathematical connection problems, the next section will present examples of cases of student difficulties for each indicator of mathematical connection.

Table 1 shows that the percentage of students who had difficulty in mathematical connections for each indicator was higher than those who had no difficulty. Although the gap between these two groups varied for the three types of problems given, the percentage of students who had difficulty always dominated those who had no difficulty. In the next section, a number of cases will be described regarding the student difficulty in mathematical connections for each indicator.

### 3.2. Different Representation (DR) As a Form of Mathematical Connection

Of the three problems given to the students, the average percentage of students who experienced difficulty for different representation (DR) indicator was $65.79 \%$. This percentage clearly shows that most students still experienced difficulty in applying this indicator. An example of student difficulty in this indicator is presented in Figure 2.

The example of student answer in Figure 2 show that this student failed to solve the problem correctly. The failure started when the student did a mistake in designing a mathematical model appropriate to the context of the problem. In step 1, the student defined two new variables namely $p$ and $q$, where $p=\frac{1}{A-2 B}$ dan $q=\frac{1}{A+2 B}$. It can be observed that these two variables could not be linked to the two initial equations found in Problem 1. In addition, in step 2, it also shows that the equation model made was out of sync with the results obtained in stage 1 . Based on this finding, it is clear that the student's problem occurred when he was not able to represent the form $\frac{A B}{A^{2}-4 B^{2}}$ into another form, and therefore incorrectly took another procedure to solve Problem 1.

Problem 1 and Solution:
If A and B meet the system
$\left\{\begin{array}{c}\frac{2 A}{A-2 B}-\frac{6 B}{A+2 B}=3 \\ -\frac{A}{A-2 B}+\frac{6 B}{A+2 B}=-1\end{array}\right.$
the value of $\frac{A B}{A^{2}-4 B^{2}}=\cdots$
Solution:


Suppose that $\frac{A}{A-2 B} \rightarrow x$ and $\frac{B}{A+2 B} \rightarrow y$, .
So:


Therefore, $\frac{A B}{A^{2}-4 B^{2}}=\frac{A}{A-2 B} \cdot \frac{B}{A+2 B}=2 \cdot \frac{1}{6}=3$
Notes:
DR IM PD : Indicators of mathematical connections

Example of student answer:


Notes
(2) 3 ( 4 : Steps of solving the $\begin{aligned} & \text { problem }\end{aligned}$

Figure 2. Example of student answer with difficulty in Different Representation (DR)

Another example of student difficulty in the different representation (DR) indicator can be seen in Figure 3. In Figure 3 [a], the error in representing a different form of trigonometric equation occurred in step 4 (inside the box). Likewise, the example of student's answer in Figure 3 [b], in the red box, it is clear that students incorrectly changed the form $\frac{\cos 2 x}{\sin 2 x}$ into $\tan x$. Meanwhile, in Figure 3 [c], the error began in step 2, where the student manipulated the form $2 \sin x \cdot \cos 2 x$ and $\cos x \cdot \sin 2 x$ by using the formula for multiplying sine and cosine. Examples of these errors provide empirical evidence that the students still encountered difficulties in the different representation (DR) indicator for solving mathematical connection problems.

Problem 2 and Solution:
If $x_{1}$ and $x_{2}$ is a solution to $\frac{2 \sin x \cdot \cos 2 x}{\cos x \cdot \sin 2 x}-$ $5 \tan x+5=0, \tan \left(x_{1}+x_{2}\right)=\cdots$

Solution:


Example of Student Answer:

[a]
(1) $\frac{2 \sin x}{\cos x} \cdot \frac{\cos 2 x}{\sin 2 x}-5 \tan x+5=0$
$2 \tan x \cdot \tan 2 x-5 \tan x+5=0$
(1) $\frac{2 \sin x \cos 2 x}{\cos x \cdot \sin 2 x}-5 \tan x+5=0$
(2) $\begin{aligned} & \frac{\sin (x+2 x)+\sin (x-2 x)}{\frac{1}{2}(\sin (x+2 x)-\sin (x-2 x))}-5 \tan x+5=0 \\ & 2 \sin 3 x+\sin (-x)\end{aligned}$
(3) $\frac{2 \sin 3 x+\sin (-x)}{\sin 3 x-\sin (-x)}-5 \tan x+5=0$
[c]

Figure 3. Another example of student answer with difficulty in Different Representation (DR)

### 3.3. Part-Whole Relationships (PWR)

In this study, the PWR indicator for solving mathematical connections problems was only found in Problem 3. The percentage of the students who did not master this indicator was the highest among all of the indicators, at $97.37 \%$. This strongly indicated that in the context of the given problem, the student ability to do part-whole relationships was still poor. Examples of student answers that indicate that they have difficulties with the PWR indicator are presented in Figure 4.

Problem 3 and Solution:
Given information: a small cricle with a radius of $3 \sqrt{2}$ intersects the center of a large circle with a radius of 6 . The line connecting the circle point is the diameter of the small cricle as illustrated in the following figure. Calculate the area of intersection between the two circles.


Problem Ilustration
Solution:
$A B=$ Diameter of small circle
Segment area of the bigger circle (A1):
Section area of $A P B=\frac{\angle A P B}{360^{\circ}} \pi r^{2}$


The section area of $A P B=\frac{90^{\circ}}{360^{\circ}} \pi \cdot 6^{2}=9 \pi$
$\mathbf{A 1}=$ The section area of $A P B-$ The area of $\triangle A P B$
$\mathbf{A 1}=9 \pi-\frac{1}{2} \cdot 6.6=9 \pi-18$


The area of $1 / 2$ small circle (A2):
$\frac{1}{2} \pi \cdot r^{2}=\frac{1}{2} \pi \cdot(3 \sqrt{2})^{2}=9 \pi \longrightarrow$ ewr
The area of intersection between the two circles:
$\mathrm{A} 1+\mathrm{A} 2=9 \pi-\widehat{18+9 \pi=18 \pi-18}$
PD

Example of student answer:


The area of $1 / 2$ small circle
$L \frac{1}{2} \odot h_{\text {ecal }}=\pi \cdot r^{2}$
$2=\pi \cdot(3 \sqrt{2})^{2}$
$2=\pi \cdot i 8$
ea of
arcle $=18 \pi$
besar $=\pi \cdot r^{2} 3$

$$
=\pi \cdot 6^{2}
$$

$=36 \pi$
Segmen area
4) Lemberang
$36 \pi-\omega \pi=\omega \pi$
The area of intersection
$L \cdot Z_{r i s a n}=18 \pi+18$

$R=6$
$r=3 \sqrt{2}$

(2) $\frac{\angle C B D}{\angle C A D}=\frac{3 \sqrt{2}}{6}$

$$
\begin{aligned}
\frac{180}{x} & =\frac{3 \sqrt{2}}{6} \\
<x & =\frac{6 \times 180}{3 \sqrt{2}} \times \frac{\sqrt{2}}{\sqrt{2}} \\
& =\frac{1080 \sqrt{2}}{6} \\
& =180 \sqrt{2}
\end{aligned}
$$

$* L C A D=\frac{180 \sqrt{2}}{360} \times \pi .36$

$$
=\frac{\sqrt{2}}{2} \times \pi 36
$$

$$
=18 \sqrt{2} \pi
$$

$*$

$$
\begin{aligned}
L C B D & =\frac{180}{360} \times \pi \cdot 18 \\
& =\frac{1}{2} \pi \cdot 18 \\
& =9 \pi \\
& {[b] }
\end{aligned}
$$

Figure 4. Example of the student answer with difficulty in Part-Whole Relationship
(PWR) indicator

Figure 4 [a] shows that in step 1, the student actually understood the meaning of Problem 3. However, it appeared that the students had difficulty to calculate the segment area of a large circle. Based on the student's answer in Figure 4 [a], the student calculated the area of a large circle segment $=$ the area of a large circle - the area of $1 / 2$ small circle. What the student did in this step indicated that he was not able to find the basic concepts used to calculate the area of a segment (such as the rules of cosine, the area of section, and the area of a triangle). In other words, the student encountered difficulty in finding part-whole relationships to find the segment range of the large circle. Likewise the example of student answer in Figure 4 [b], from a series of procedures carried out by the student to solve Problem 3, it can be seen that the student found it hard to analyze the parts (see step 1) or the basic concepts used to find the whole solution to Problem 3 (see step 2 and step 3).

### 3.4. Connections Where A Implies B (IM)

IM indicator in mathematical connections is operationally visible when students are able to show a relationship that a mathematical concept results in another concept. In the three problems given to the students, each procedure for solving these problems contains an IM indicator. Based on the test, of the three problems containing the indicator, there were only $30.70 \%$ of the students who mastered the indicator, while the remaining $69.30 \%$ of the students did not master the indicator. The examples of student answers with difficulties in the connections where A implies B (IM) indicator are presented in Figure 5.

[a]

Example of Student Answer for Problem 2:

$1-\tan ^{2} x-5 \tan x+5=0$
$\tan ^{2} x+5 \tan x-6=0$
$\begin{aligned} & \text { misal } \tan x=y \\ & y^{2}+5 y-6=0 \\ &(y+6)(y-1) \\ & x_{1}=-6 \quad x_{2}=1 \\ & \tan \left(x_{1}+x_{2}\right)=-6+1 \\ &=-5\end{aligned}$
[b]

Figure 5. Example of student answer with difficulty in Connections Where A Implies B (IM) indicator

From algebra theory, the student's work in Figure 5 [a] was correct, but it was ineffective and requires more time to find the final answer. If we compare the student's answer in

Figure 5 [a] with the solution to Problem 1 (see Figure 2), the difference is very clear. The student's work in Figure 5 [a] clearly showed that he/she was not able to simplify the equations given. This is because the student was not able to manipulate the form from $\frac{A B}{A^{2}-4 B^{2}}$ into $\frac{A}{A-2 B} \times \frac{B}{A+2 B}$. As a result, the student failed to find another simpler concept (for example, doing mathematical modelling) leading to the discovery of the concept of a two-variable linear equation system (SPLDV). If the student succeeds in finding a simpler form of SPLDV of the two equations given, the procedure for solving Problem 1 will be easier.

Meanwhile, as seen in Figure 5 [b], the student made a mistake in step 6. In this step, the student assumed/defined $\tan x=y$, so the trigonometric equation in step 5 could be changed into a quadratic equation $y^{2}+5 y-6=0$. By dividing it into factors (factorizing), the solutions from the quadratic equation were $y=-6$ dan $y=1$ (in Figure $6[b]$ the student wrote the solution as $x_{1}=-6$ and $x_{2}=1$ ). In this case, the solution of the quadratic equation found should be changed into the solution for the trigonometric equation. Because the student previously defined $\tan x=y$, the solution of the quadratic equation is converted into $\tan x=-6$ and $\tan x=1$. Due to some errors in performing the procedure, the final solution for determining the value of $\tan \left(x_{1}+x_{2}\right)$ was also incorrect. From this case, it is clear that the students still had difficulty in connecting a mathematical concept that results in other concepts.

### 3.5. Connections showing that $A$ is a procedure for doing $B$ (PD)

Another difficulty experienced by the students in mathematical connections is related to the indicator of connections showing that $A$ is a procedure for doing $B$ (PD). If the students were able to show that a mathematical procedure is applied to obtain another procedure, they were considered to be competent at this PD indicator. Each of the three problems tested contained the PD indicator and it was obtained that the average percentage of the students who experienced difficulties for this indicator was $74.56 \%$. The examples of student answers with difficulty in PD indicator can be seen in Figure 6.

In Figure 6 [a], the student was able to find a solution to the trigonometric equation (see step 4 and step 5) resulted from the previous process, even though they did not assume first that $\tan x=x$. However, some errors still occurred in step 7 and step 8 , when the student associated that the value of $x$ is the angle (see step 7). The angles were then substituted with the equation $\tan \left(x_{1}+x_{2}\right)$ (see step 8 ), even though the intended final solution from Problem 3 was different. This clearly showed that the student was not able to connect between the procedures performed in steps 4,5 , and 6 with the equation $\tan \left(x_{1}+x_{2}\right)($ step 8$)$. Likewise the student's answer in Figure $6[\mathrm{~b}]$, when the student calculated the area of a section (see step 3, inside of the box), they wrote that the section area of the large circle was $\frac{90^{\circ}}{360^{\circ}} \times$ area of a large circle. However, the students did not show what procedure was applied to find a $90^{\circ}$ angle. According to the illustration drawn by the student (see step 1), a $90^{\circ}$ angle was determined based on the assumption that the triangle formed was a right triangle, not associated with cosine rules (see solution to Problem 3 in Figure 4). This showed that the students were not able to show what procedure should be previously applied to calculate the section area of the circle.

Example of Student Answer for Problem 2:

[a]

Example of Student Answer for Problem 3:


(5) $=\frac{1}{4} \pi \cdot 6^{2}-\frac{6.6}{2} \quad \frac{\text { Base } \times \text { height }}{2}$
(6) $=\frac{36}{4} \pi-\frac{36}{2}$
(7) $=9 \pi-18$
[b]

Figure 6. Example of student answer with difficulty in Connections showing that $A$ is a procedure for doing B(PD) indicator

## 4. Discussion

The results of this study support the findings of several previous studies which show that the students still experience difficulties in mathematical connection (DoloresFlores, et al., 2018; Kenedi, et al., 2019; Lapp, et al., 2010; Siregar and Surya, 2017). Although the results of previous studies involved participants at different levels, from elementary school to undergraduate levels, the obstacles faced by each participant were almost the same in general, including the difficulty in making representations in other forms, doing part-whole relationships, making implications, and showing the interrelationships between mathematical procedures. These mathematical connection difficulties also occurred in this study.

One of the key factors in making mathematical connection is deep understanding of its concept (Dolores-Flores, et al, 2018; García-García \& Dolores-Flores, 2017; Silver, et al, 2009) and obtaining such conceptual understanding also needs mathematical connections (Anthony \& Walshaw, 2009). Poor understanding of concepts is therefore believed to be the main cause of the students' difficulty of making mathematical connections (Dolores-Flores, et al, 2018). As also confirmed from the interview conducted in this study, almost all of the students experiencing difficulties in making mathematical connections claimed that they did not understand mathematical concepts needed to solve mathematical connection problems. For that reason, mathematics instruction in the classroom should be focused on how to instill mathematical concepts in students in order to develop other mathematical skills.

Lack of familiarity with mathematical connection problems also caused difficulties in solving the problems. Mhlolo et al. (2012) suggest that most students lack the opportunity to deepen understanding of mathematical connections. In addition, the books used have not yet been linked specifically the materials with various contexts, mathematics with real-life, and thus hinder the students to develop their mathematical connection skills (Salout et al., 2013). In this case, Baki et al. (2009) recommend the need to make changes in the mathematics class in terms of the content and context that must be applied.

The teacher's pedagogical competence in training the students to solve mathematical connections also needs immediate attention. It is important to ensure that the teacher is well prepared and have confidence that the students have sufficient initial abilities to develop various mathematical skills. Bowen (2014) reports that teachers tend to be hesitant about using their knowledge of mathematical connections because they doubt their student abilities (Bowen, 2014). For this reason, instilling confidence in teachers that their students are able to develop their ability in mathematical connection is very important. Besides, lack of assistance among the teachers regarding the planning and implementation of learning that facilitates students to make mathematical connections (Monroe \& Mikovch, 1994) is of concern especially to policy makers in the field of education.

Various efforts can be made to improve student ability in mathematical connections include the following: applying Problem-Based Learning (PBL) in mathematics learning (Kartikasari \& Widjajanti, 2017; Malasari et al., 2017); applying collaborative problembased learning strategy (Widjajanti, 2013); using varied methods in learning such as direct learning, demonstration, practice and exercise, and also using modified instructional media (Jannah et al., 2017). In addition, it is important to give the students more activities of problem solving in order that they make a habit of it. Students of all ages are more motivated with problem situations that involve them and their classmates (Welchman-Tischler, 1992); use three-dimensional manipulatives (Safi \& Desai, 2017); and use proof approaches (Jiang \& O'Brien, 2012). Another strategy that can be applied is using writing strategies in learning mathematics such as making drawings, pictures, tables, and graphs; providing clear explanation of problem-solving methods and justifications of processes; and doing reflection on learning (Haltiwanger \& Simpson, 2013).

## 5. Conclusions and Implications

Based on the results of the study and discussion, it can be concluded that the students still experienced difficulties in mathematical connections. These difficulties included different representation as a form of mathematical connections, part-whole relationships, connections that show A is a procedure for doing B (relationships between procedures of mathematics). In general, the indicators of mathematical connection difficulties experienced by the students were: (1) lack of familiarity in solving mathematical connection problems characterized by difficulties in reading mathematical patterns, linking between mathematical concepts, and working out mathematical manipulations; (2) poor understanding of the concept characterized by difficulties in understanding some mathematical terms, comprehending the whole
problem, identifying important points of the problem, applying mathematical formulas; and (3) lack of interest in word problems. The results of this study imply that mathematics instruction needs improvement in order to increase students' abilities to solve mathematical connections. For this reason, we recommend that mathematics teachers create innovation in mathematics instruction by using various approaches or learning models that can practice students' mathematical connections such as problembased learning, creative problem solving and other constructivist learning models. In addition, improving the quality of mathematics teaching materials also needs considerable attention. We recommend that the materials used to teach mathematics contain problem solving activities that link a number of mathematical concepts and procedures, and also connect mathematics with other disciplines and real-life situations. Regarding the limitations of this study, we suggest that future research investigate difficulties experienced by students in mathematical connections by involving a large number of participants to obtain broader generalizations. Furthermore, conducting research and development in learning materials used to practice mathematical connections is also urgently needed.

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## Bukti Permintaan Revisi Artikel

## [IJLTER] Editor Decision

## 10 pesan

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Kepada: Jailani Jailani [jailani@uny.ac.id](mailto:jailani@uny.ac.id)
Cc: Heri Retnawati [heri_retnawati@uny.ac.id](mailto:heri_retnawati@uny.ac.id), Ezi Apino [apinoezi@gmail.com](mailto:apinoezi@gmail.com), Agus Santoso [aguss@ecampus.ut.ac.id](mailto:aguss@ecampus.ut.ac.id)

Jailani Jailani:
We have reached a decision regarding your submission to International Journal of Learning, Teaching and Educational Research, "Do the Students Experience Difficulties in Mathematical Connections to Solve Mathematical Problems?".

Our decision is to: accept the paper if the requested changes are made

## IJLTER .ORG <br> ijlter.org@gmail.com

## Reviewer B:

Paper length::
Ok
Originality::
Good
Scope of paper::
Relevant to IJLTER
Related work::
Acceptable
Language::
The language is clear and understandable.
References::
There are enough references and reliable.
Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:

The topic is very relevant and current. However the research involves not only phenomenology but also used quantitative data. May I then suggest that the researchers may use Explanatory research design by which involve initially with quantitative analysis followed by qualitative analysis of data.

## Reviewer D:

Paper length::
Ok
Originality::
Good
Scope of paper::
Relevant to IJLTER

Related work::
Acceptable
Language::
already good

## References::

Ok
Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:

Some suggestions in the article comments
see 10293

Reviewer F:
Paper length::
Ok
Originality::
Acceptable
Scope of paper::
Highly relevant
Related work::
Acceptable
Language::
Good, but needs some improvement. Please see comments in the reviewed paper.

## References::

Very Good
Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:

1. Please consider revising the title into "High School Students'

Difficulties in Mathematical Connections when Solving Problems"
2. Please make the tense of the verb consistent in the Literature review
3. Please provide more details in Methods section. Please the comments in the reviewed paper.
4. Please include in the Discussion the possible reasons the students experienced the greatest difficulty in PWR, wherein 30 of the 31 students had experienced difficulties in this mathematical connection. Could the mathematics achievement or ability of these students be related to their difficulties? Did previous studies find similar or contrasting results? You may also relate metacognitive ability as an indicator of successful problem solver. Students who rarely exhibit metacognitive skills fail to solve nonroutine problems and therefore encountered difficulties in mathematical connections. See for example Nool (2011) at https://www.academia.edu/43336452/ and Bas (2016) at https://files.eric.ed.gov/fulltext/EJ1105294.pdf
5. The Reference list is complete and well-written. Just insert "\&" in the entry Leikin, R., Pitta-Pantazi, D. (2013)

Your research topic is interesting and contributes to existing body of knowledge on mathematical connections and problem solving. Congratulations! see 10242

Reviewer H :
Paper length::

Originality::
Acceptable
Scope of paper::
Relevant to IJLTER
Related work::
Poor

## Language:

/* In general, the English in the present manuscript is of publication quality and require minor improvement. Please carefully proof-read spell check to eliminate grammatical errors

## References::

This paper provides a somewhat dated and shortlist of literature, related to the need of the proposed study. The paper needs a more comprehensive literature review and coherent studies reflecting the current state of the art.

Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:

Abstract
The abstract generally explains the study and its rationale clearly. The recommendations could use some honing. It would be desirable for the final section in the paper to mention which aspects of the study would cross-apply to professional environments and why the results can be extrapolated beyond educational coursework. The Methodology component of the abstract should clarify the types of data analytics used.

## Introduction

This research would acquire more relevance and impact if it noted some of the emerging trends and pressures that could inhibit collaborations from being a learning experience.

## Literature Review

Regarding the research base of the study, the literature review is thorough. The findings of previous research are engaged thoughtfully and analyzed critically. The literature could use some updating.
Furthermore it is well known that longitudinal research indicates that low attainment in mathematics can have significant long-term consequences, affecting later school achievement, employment, criminality, mental health and future earnings. In many countries, underachievement in mathematics is strongly associated with social, cultural and economic disadvantage. Children think mathematically long before they start school and mathematical thinking is a strong predictor for later academic success in school indeed, it is a better predictor than early reading and early attention skills. Mathematics really is fundamental to a child's development \& communication in later life. Basic numeracy skills assist kids in terms of achievement \& just being a competent adult. A broader acknowledgement of this would lead to more parity with literacy. However, developing a strong foundation in early math skills is vital for children's later educational success and economic, health, and employment outcomes. Children who enter school with strong mathematics skills have a greater likelihood of success in mathematics in kindergarten and in later grades.
It is suggested that the author(s) can consider the following papers related to necessity of mathematical education, the use or realistic mathematics to promote 21 st century skills, etc. to strengthen the background and conclusions of the study:

Papadakis, S., Kalogiannakis, M., \& Zaranis, N. (2016). Comparing tablets and PCs in teaching mathematics: An attempt to improve mathematics competence in early childhood education. Preschool and Primary Education, 4(2), 241-253.
Papadakis, S., Kalogiannakis, M., \& Zaranis, N. (2018). The effectiveness of computer and tablet assisted intervention in early childhood students'
understanding of numbers. An empirical study conducted in Greece. Education and Information Technologies, 23(5), 1849-1871.
Papadakis, St., Kalogiannakis, M., \& Zaranis, N. (2016). Improving
Mathematics Teaching in Kindergarten with Realistic Mathematical Education. Early Childhood Education Journal, 45(3), 369-378.

## Methodology

The explanation of the research process and the results could be explained more thoroughly to make the study more transparent and informative, as the subsequent commentary details.
Findings
On the reporting of results, the associated data merit further attention.

## Discussion

In general, the discussion of results could adopt a more critical, analytical perspective to supplement and strengthen the descriptive reporting of the data.
Regarding the limitations and reflections, the authors could profitably dig more deeply into some of the variables that might or might not have come into play in generating the results.

Conclusion.
The finding should be related to results from previous literature. The conclusion section should highlight the unique contributions of the paper and the limitations of the research. Discussions on what should be done in the future are useful. The discussion and conclusion should make it clear how the research findings contribute to new knowledge.
Overview:
Paper needs a stronger literature review and comparison to the other studies in the same study area. The research is interesting, but a revision of the paper is required to make it presentable in a research journal.

## Reviewer K:

Paper length::
Ok
Originality::
Good
Scope of paper::
Relevant to IJLTER
Related work::
Acceptable
Language::
OK
References::
OK
Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:

OK
see 10126

Reviewer L:
Paper length::
Quite long
Originality::
Acceptable

Scope of paper::
Relevant to IJLTER
Related work::
Acceptable
Language::
it is suggested to check some punctuation marks
References::
no comments
Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:
see 10194

## Reviewer M:

Paper length::
Ok

Originality::
Good
Scope of paper::
Relevant to IJLTER
Related work::
Acceptable
Language::
the write ups is ok
References::
the reference is ok
Additional comments along the following lines: originality, literature
review, methodology, evaluation of results, research implications, quality
of communication, etc.:
The are items in the methodology need to address please the comment section...
see 10132

## Reviewer N :

Paper length::
Ok
Originality::
Acceptable
Scope of paper::
Relevant to IJLTER
Related work::
Acceptable
Language::
The language is acceptable.

## References::

References are good and correct format.

Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:
(1)Paper format, font size, alignment and reference list order should be strongly emphasized. And more guidelines are available on IJLTER Journal website.
(2)Need to add at least 5 keywords.
(3)Need to discuss more detail for the comparison between the students who had mastered and those who faced difficulties of mathematical connection.
(4)According to figure 1, the author needs to be detailed that the number of unskilled students is greater than the number of skilled students in every problem.
(5)Findings and discussions should be presented more detail and visible.

Reviewer O:
Paper length::
Ok

Originality::
Acceptable
Scope of paper::
Relevant to IJLTER

## Related work::

Acceptable
Language::
well understanding
References::
give the newest references (up to date sources)
Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:
on the result and discussion, discuss the position of student's mastery that you interviewed, give the learning theory that support your solution (problem based learning).

## Reviewer Q:

Paper length::
Ok
Originality::
Very innovative
Scope of paper::
Highly relevant
Related work::
Excellent

## Language::

The command of language is very good and the facts are presented coherently. This shows how the authors are in good stead in scholarly work.

## References:

The authors used strong references for their literature resources with over $40 \%$ of their list within the last five years. However, it could have been
better if the recent literature sources are improved to about $75 \%$ of them being within the last five years. There was an old reference book (Bogdan R C \& Biklen S K (1982), being too old unless a more recent edition of the same book is considered. There have been alot done for the last 38 years in Qualitative Research worth being cited. I suggest this be reviewed too.

Additional comments along the following lines: originality, literature review, methodology, evaluation of results, research implications, quality of communication, etc.:

The research design and methods were matching the objective of the study.
The findings demonstrated that the research achieved expected goals. However, the author(s) felt short of explaining the population size and how the sample size, 31, was arrived at. If there was some criteria adopted, I believe that could have been boldly covered in the write-up. I suggest that to be included in the review. I also advise that labeling is reviewed e.g. 4[a] wasn't done well.

## International Journal of Learning, Teaching and Educational Research

http://ijlter.org/index.php/ijlter

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4 September 202006.25
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[aguss@ecampus.ut.ac.id](mailto:aguss@ecampus.ut.ac.id)
Dear Authors,

## The decision for your paper is: accept the paper if the requested changes are made

You need to do the following and submit the paper by email by 15 th September 2020 for possible publication in the August 2020 issue if all the requested changes are made. The paper will undergo another review process to make sure all requested changes have been incorporated as far as appropriate before the final acceptance decision is taken.

## Editor's Note

1. Format the paper strictly according to the template (attached).

Add the orcid of all authors. If you do not have one, please create it on orcid.org
2. Follow APA style strictly for the references. References must strictly follow APA format 6th edition, otherwise publication will be delayed.
http://www.apastyle.org/
http://student.ucol.ac.nz/library/onlineresources/Documents/APA_guide_2015.pdf
3. Check if references are mentioned in the text (and vice-versa). The paper must have at least 30 references. Failure to correct the references will delay the review process.
Also include recent papers (2015-2020) in the references (if need be).
Any non-English words must have their equivalent inside square brackets [].
References must be ordered in alphabetical order.
When writing the references in APA style, please pay attention to all details. Everything matters to us (a space, a comma, a full-stop, a bracket, a hyphen, lowercase vs uppercase, etc, etc).
4. Address all the concerns of the reviewers, as far as appropriate.
5. Mention the doi of each reference where available.
a. Go to http://search.crossref.org/
b. Copy and paste the title of the paper in the search box
c. Press the Enter key.
d. Copy and paste the doi back to the paper (into the reference section) is one is available. DOI may not be available for some of the references. This is fine.
e. There are two ways you can write the doi (1) doi:10.1037/a0028240 or (2) http://dx.doi.org/10.1037/a0028240
6. Prepare a separate word document to indicate the changes that were made as a result of each reviewer's comments. This is compulsory. The revised paper will not be considered without this. You must explain how you responded to EACH comment from EACH reviewer. A template is attached. It does not suffice to write done or fulfilled next to a review comment. You need to explain in detail how the comment was responded to and provide page numbers as well. Also highlight the changes made in the paper.
7. Paper must be at least 5500 words (inclusive of references) and must NOT exceed 10,000 words.
8. The abstract must be between $175-250$ words. The abstract must preferably be in one paragraph only.
9. The conclusion must be between $175-300$ words. One or two paragraphs is preferred but not compulsory. Avoid numbering in conclusion.
10. You are strongly advised to use Grammarly to check your paper. Create an account in Grammarly.com and upload your paper. You can use the free version. It will catch the obvious mistakes (if any). You should decide what to change and what to keep at it is (most alerts are just suggestions which could be ignored). You also have a MS Word add-in for Grammarly. It is attached to this email. You can install it and then open MS Word. You will see a new item in the menu. You will need to login with your Grammarly account credentials to access the services. A good score is above $97 \%$. The higher the better. You should not use a mixture of British and American English (for example behavioral v/s behavioural). You should use only one type of English. You can also use MS Word Editor to make further corrections. Avoid using long sentences. Consider splitting them into two or more sentences. The report is attached.
You are advised to have the paper edited by a professional English language editor. This is not compulsory if you feel that your English is already at a very good level.
One good service is: https://www.proofers.co.uk/editing-process/
We are not affiliated in any way with them but we know that they do a great job, through our authors.

## 11.Similarity score is ok.

12. If you have any supplementary files (such as survey questionnaire), please send them to us via email or include them in your main paper (recommended).

The paper will undergo a second round of review to ensure that all requested changes were made to the full satisfaction of the reviewers and IJLTER.

Failure to make the requested changes will delay the publication of the paper.
Note that our publication fees are $\$ 450$ USD for papers less than 8,000 words.
http://ijlter.org/index.php/ijlter/about/submissions\#authorFees
If you have any queries, please let us know.
Prof. Antonio Sprock
CE

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International Journal of Learning, Teaching and Educational Research

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Dear Authors,
When are you planning to submit the revised paper?
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- jailani [jailani@uny.ac.id](mailto:jailani@uny.ac.id)

13 September 202012.52
Kepada: IJLTER ORG [ijlter.org@gmail.com](mailto:ijlter.org@gmail.com)

## Dear Editor,

Thank you for your email. We plan to submit the revised paper on Monday, September 14, 2020. Thank you very much for your attention.

## Best regards

Jailani
[Kutipan teks disembunyikan]

IJLTER ORG [ijiter.org@gmail.com](mailto:ijiter.org@gmail.com)
Kepada: - jailani [jailani@uny.ac.id](mailto:jailani@uny.ac.id)

Noted with thanks.
[Kutipan teks disembunyikan]
[Kutipan teks disembunyikan]
Untuk mendukung "Gerakan UNY Hijau", disarankan tidak mencetak email ini dan lampirannya.
(To support the "Green UNY movement", it is recommended not to print the contents of this email and its attachments)
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- jailani [jailani@uny.ac.id](mailto:jailani@uny.ac.id)

14 September 202015.42
Kepada: IJLTER ORG [ijlter.org@gmail.com](mailto:ijlter.org@gmail.com)
Dear Editor,
Hope you are doing well today. Herewith this email, we attached the revised paper and Response to Reviewers file. We hope the Editors can follow up on that. Thank you very much.
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Hope you are doing well today. Herewith this email, we attached the revised paper and Response to Reviewers file. We hope the Editors can follow up on that. Thank you very much.

Best Regards
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Pada tanggal Min, 13 Sep 2020 pukul 12.54 IJLTER ORG [ijlter.org@gmail.com](mailto:ijlter.org@gmail.com) menulis:
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14 September 202015.45
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IJLTER ORG [ijlter.org@gmail.com](mailto:ijlter.org@gmail.com)
16 September 202010.48
Kepada: - jailani [jailani@uny.ac.id](mailto:jailani@uny.ac.id)
Dear Dr Jailani,
Thank you for making the requested changes and for submitting the final paper. It is now ready for publication after a final assessment has been made.

Our copy-editing team will do the final formatting before publication.
You can now make the payment of $\$ 500$ using the following link:
https://www.paypal.me/LondonConsultingLtd/500
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Prof. Antonio Sprock
CE
[Kutipan teks disembunyikan]

- jailani [jailani@uny.ac.id](mailto:jailani@uny.ac.id)

Kepada: - heri_retnawati [heri_retnawati@uny.ac.id](mailto:heri_retnawati@uny.ac.id), "Janu Arlinwibowo januarlinwibowo.2018"
[januarlinwibowo.2018@student.uny.ac.id](mailto:januarlinwibowo.2018@student.uny.ac.id)

From: IJLTER ORG [ijlter.org@gmail.com](mailto:ijlter.org@gmail.com)
Date: Wed, 16 Sep 2020, 10:48

Subject: Re: [IJLTER] Editor Decision
To: - jailani [jailani@uny.ac.id](mailto:jailani@uny.ac.id)
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## Komentar Reviewer dan Perbaikan yang Dilakukan

International Journal of Learning, Teaching and Educational Research (IJLTER)
Response to Reviewers' Form
Title of Paper: Do the Students Experience Difficulties in Mathematical Connections to Solve Mathematical Problems? (Before the revision)

High School Students' Difficulties in Making Mathematical Connections when Solving Problems (After the revision)

Paper ID: 2606-9918
Number of Reviewers: 10 (Ten)

| Reviewer 1 |  |  |  |
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| \# | Reviewer's comments | Response | Page <br> No. |
| 1 | The topic is very relevant and current. However, the research involves not only phenomenology but also used quantitative data. May I then suggest that the researchers may use Explanatory research design by which involve initially with quantitative analysis followed by qualitative analysis of data. | We appreciate this suggestion, but if we change our research design, it may change the nature and focus of the study. In this study, our focus is to explore the phenomena related to the obstacles faced by students when solving math problems, so we think that the phenomenological approach is more appropriate. To accommodate the reviewer's suggestion, we did not change the research design explicitly, but we did sharpen the data analysis technique, which began with quantitative analysis and followed by qualitative analysis, as mentioned by the reviewer. A more detailed explanation can be seen in the Data Analysis subsection. | 6-8 |
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| Reviewer 2 |  |  |  |
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| \# | Reviewer's comments | Response | $\begin{array}{\|l} \hline \text { Page } \\ \text { No. } \\ \hline \end{array}$ |
| 1 | Do Students Experience.....Problems? | We remove "the" before the word "Students" in the title and change the title as suggested by Reviewer 3. <br> Before: <br> Do the Students Experience <br> Difficulties in Mathematical <br> Connections to Solve Mathematical <br> Problems? <br> After: <br> High School Students' Difficulties in Making Mathematical Connections when Solving Problems | 1 |
| 2 | What is the theory basis for this grouping? It has not been explained: <br> 1. Low Mastery value range <br> 2. Average Mastery value range <br> 3. High Mastery value range where do these values come from? Please explain | We have added a detailed explanation regarding the grouping of students' abilities in the Data Analysis Section. Our explanation can be found in Paragraphs 2 to 4 of the Data Analysis Techniques Section. | 6-7 |
| 3 | where do these percentages come from? Please explain | We have provided an explanation regarding the percentage in the data analysis section. Our explanation can be found in Paragraph 5 of the Data Analysis Techniques Section. <br> In body text: <br> The data obtained were then tabulated based on the students' ability categories (High Mastery, Average Mastery, and Low Mastery) and mathematical connection indicators (DR, PWR, IM, and PD) for each problem. From this tabulation, we obtained the number and percentage of students for each category of ability and mathematical connection indicators for each problem. ... | 7 |
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| Reviewer 3 |  |  | Response |
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| \# | Reviewer's comments | Page <br> No. |  |
| 1 | Please consider revising the title into <br> "High School Students' <br> Difficulties in Mathematical Connections <br> when Solving Problems" | We have considered a suggestion <br> from Reviewer 3. <br> Before: <br> Do the Students Experience <br> Difficulties in Mathematical <br> Connections to Solve Mathematical <br> Problems? | 1 |
| 2 | Please make the tense of the verb <br> consistent in the Literature review | After: <br> High School Students' Difficulties in <br> Making Mathematical Connections <br> when Solving Problems | We have made improvements in the <br> use of tense in the literature review. <br> To ensure that, we also check <br> through Grammarly. |
| 3 | Please provide more details in Methods <br> section. Please the comments in <br> the reviewed paper. | We have added some more detailed <br> explanations to the methods section, <br> for example, the characteristics of <br> the participants, technical <br> implementation of tests and <br> interviews, data analysis techniques, <br> etc. | 5 -7 |
| 4 | Please indicate the grade or year level of <br> the students. Do they have the same grade <br> or year level? <br> How many students came from school <br> with high academic achievement? From <br> medium achieving school? From low <br> achieving school? <br> It would be interesting to relate the <br> mathematical achievement of the students <br> on their performance in problem solving <br> and the difficulties in mathematical <br> connection when they solve problems. | We have provided a more detailed <br> explanation regarding the grade <br> level of participants and the <br> distribution of participants for each <br> school category in the Data <br> Collection section. <br> In body text: <br> The participants of this study were 31 <br> eleventh grade high school students <br> from five schools in Yogyakarta Special <br> Region and Central Java Province, <br> Indonesia. We selected the schools as <br> representatives with high, medium, <br> and low academic achievement. Six <br> students came from school with high <br> academic achievement, 21 students <br> came from school with medium <br> academic achievement, and 12 <br> students came from school with low <br> academic achievement. When we <br> conducted the study, the students <br> involved in this study were between 15 <br> and 17 years old. | 5 |


| 5 | Please provide a description of the <br> qualifications and teaching experience or <br> position of this expert. | We have provided an explanation <br> regarding the qualifications and <br> experience of the experts who are <br> validators of our instruments. The <br> explanation can be found in <br> Paragraph 1 in the Data Collection <br> subsection. <br> In Body text: <br> The validity of the test instrument was <br> proven through content validation by <br> asking experts to agree on the item's <br> suitability with the indicators. The <br> experts were two high school <br> mathematics teachers and two <br> mathematics education lecturers.... | 5 |
| :--- | :--- | :--- | :--- |
| 6 | Please indicate the number of minutes or <br> hours the students took the test. Did they <br> take it in regular classroom during their <br> class time or in a separate room during <br> their vacant or available time? | We have added information <br> regarding test duration and <br> technical implementation in the <br> Data Collection subsection. | 6 |
| 7 | In Body text: | Were the interviews conducted right after <br> The test was not administered in the <br> regular classroom but taken vacant or <br> available time as agreed by the teacher, <br> students, and researchers in each <br> school. We gave students 30 minutes <br> individually or by group? <br> About how many minutes did each <br> interview last? <br> Were the interviews audio recorded or <br> other modes of recording were done? | We have added information related <br> to technical interviews, duration, <br> and recording methods in the Data <br> Collection subsection. |
| How did you ensure the reliability and <br> validity in interpreting qualitative data? <br> Was there an expert apart from the <br> researchers that validated the accuracy of <br> analysis of qualitative data? | In body text: <br> We conducted interviews with the <br> students right after they finished the <br> test. ... We conducted interviews right <br> after all students have completed the <br> mathematical connection test in each <br> school. Students have interviewed <br> alternately one by one for about 15 <br> minutes. The answers of each student <br> during the interview were noted <br> directly by the researchers. | We have provided an explanation <br> regarding the actions taken by <br> researchers to ensure the reliability <br> and validity of interpreting <br> qualitative data through Focus <br> Group Discussions involving <br> external experts. More details can be <br> seen in the last paragraph of the <br> Data Analysis subsection. | 7 |


|  |  | In body text: <br> This study involved all researchers during the data analysis processes to ensure the validity and reliability in interpreting the qualitative data. All researchers had experienced in the field of qualitative research, especially related to educational issues. Then we discussed the results of the data analysis in a Focus Group Discussion (FGD) involving all researchers and two experts. The two experts were lecturers outside the researchers' institution and had experienced in qualitative research related to educational issues. The FGD discussed research findings and its suitability and consistency with the data obtained from participants. |  |
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| 9 | Please include in the discussion the possible reasons the students experienced the greatest difficulty in PWR, wherein 30 of the 31 students had experienced difficulties in this mathematical connection. Could the mathematics achievement or ability of these students be related to their difficulties? Did previous studies find similar or contrasting results? | We have added a discussion on the PWR indicator. This discussion can be found in Paragraph 3 in the Discussion section. <br> In body text: <br> Of the four mathematical connection indicators studied in this study, most students had difficulty making the partwhole relationship (PWR). This finding is consistent with the findings of Mhlolo (2012) and García-García and Dolores-Flores (2020). When doing PWR in solving mathematics problems, students should see the connection between general concepts through specific parts in the form of particular examples (Mhlolo, 2012). In this case, we understand that students are considered capable of making PWR if they apply specific concepts or procedures properly as part of the general concept to be completed. However, in this study, most students failed to do this. To overcome it, according to Mhlolo (2012), students need to be accustomed to doing and expressing generalizations both through deductive and inductive reasoning patterns. When students have good deductive and inductive reasoning skills, we expect that they will be able to do PWR well when solving mathematics problems. | 18 |

$\left.\begin{array}{|c|l|l|c|}\hline 10 & \begin{array}{l}\text { The Reference list is complete and well- } \\ \text { written. Just insert "\&" in the } \\ \text { entry Leikin, R., Pitta-Pantazi, D. (2013) }\end{array} & \begin{array}{l}\text { We've fixed it. } \\ \text { Before: } \\ \text { Leikin, R., Pitta-Pantazi, D. (2013). } \\ \text { Creativity and mathematics education: } \\ \text { The state of the art. ZDM Mathematics } \\ \text { Education, 45, 159-166. } \\ \text { https://doi.org/10.1007/s11858-012- } \\ \text { 0459-1 } \\ \text { After: }\end{array} & 22 \\ \text { Leikin, R., \& Pitta-Pantazi, D. (2013). } \\ \text { Creativity and mathematics education: The } \\ \text { state of the art. ZDM Mathematics } \\ \text { Education, 45, 159-166. } \\ \text { doi:10.1007/s11858-012-0459-1 }\end{array}\right)$

|  | ewer 4 |  |  |
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| \# | Reviewer's comments | Response | Page No. |
| 1 | This paper provides a somewhat dated and shortlist of literature, related to the need of the proposed study. The paper needs a more comprehensive literature review and coherent studies reflecting the current state of the art. | We appreciate this suggestion. To accommodate this, we have added and refined the literature review in the Introduction section. Several things that we add and strengthen such as the importance of problemsolving in mathematics learning (can be seen in Paragraphs 2 and 3), the relationship between problemsolving and mathematical connections (Paragraph 3), the role of mathematical connections in mathematics learning (Paragraph 4), the urgency of the study (Paragraph 8), the novelty of the study compared to previous research (Paragraph 9). Besides, we added the latest references to strengthen the theoretical studies (e.g., Albay, E. M. (2019). English, L. D., Gainsburg, J. (2016). García-García, J., \& Dolores-Flores, C. (2020). Hadi, S., Retnawati, H., Munadi, S., Apino, E., \& Wulandari, N. F. (2018). Osman, S., Yang, C. N. A. C., Abu, M. S., Ismail, N., Jambari, H., \& Kumar, J. A. (2018). Özgen, K. (2016). Palmér, H., \& Van Bommel, J. (2020). Payton, S. (2019). etc.) | 2-5 |
| 2 | The abstract generally explains the study and its rationale clearly. <br> The recommendations could use some honing. It would be desirable for the final section in the paper to mention which aspects of the study would cross-apply to professional environments and why the results can be extrapolated beyond educational coursework. <br> The Methodology component of the abstract should clarify the types of data analytics used. | We appreciate comments from the reviewer. However, we cannot mention our recommendations explicitly to the abstract due to the limited words count. We highlight the recommendations explicitly in the discussion and conclusion sections. <br> We have mentioned the types of data analyzed in the abstract section. <br> In body text: <br> Data analysis began with analyzing all students' answers in solving mathematical problems and categorizing the types of difficulties experienced by students. Thematic analysis of the interview data was conducted to reveal the causes of difficulties experienced by students when making mathematical connections | 1 |
| 4 | Regarding the research base of the study, the literature review is thorough. | We have reviewed some relevant studies and made comparisons | 4 |


|  | The findings of previous research are engaged thoughtfully and analyzed critically. The literature could use some updating. | regarding what has been done and the findings. Next, we justify what makes our study differs from these studies. A detailed explanation can be found in Paragraph 9 in the Introduction section. We have also updated some references in our literature review (highlighted in yellow) <br> In body text: <br> Even though there have been many studies related to mathematical connection, there are still a few studies that are focused on investigating the difficulties experienced by students in making mathematical connections when solving mathematics problems. The study of García-García and DoloresFlores (2018) is more focused on exploring the types of mathematical connections made by high school students in performing Calculus tasks. Furthermore, the study of GarcíaGarcía and Dolores-Flores (2020) also explores the types of mathematical connections in solving Calculus application problems but involves preuniversity. Payton (2019) conducted a study that focuses on interventions that aim to develop mathematical connections. Zengin (2019) tested the use of GeoGebra software for the development of mathematical connections skills. Other studies were conducted to explore mathematical connections involving various representations (e.g., García-García \& Dolores-Flores, 2018; Mhlolo, 2012; Mhlolo et al., 2012; Moon, Brenner, Jacob, \& Okamoto, 2013). Based on this review, we are motivated to explore students' difficulties in making mathematical connections, especially when students interconnect mathematical concepts or procedures when solving mathematics problems. |  |
| :---: | :---: | :---: | :---: |
| 5 | The explanation of the research process and the results could be explained more thoroughly to make the study more transparent and informative, as the subsequent commentary details. | We appreciate the reviewers' comments. To clarify our research process, we have provided a more detailed explanation of our research procedures in the methodology section. What Reviewer 4 suggests is | 5-7 |


|  |  | the same as some of the suggestions <br> from other reviewers. These <br> improvements can be seen in detail <br> in the Participant, Data Collection, <br> and Data Analysis subsection. <br> We have also provided more <br> detailed information related to <br> study results, such as providing <br> more detailed information through <br> the chart in Figure 1. |
| :--- | :--- | :--- |
| 6 | On the reporting of results, the associated <br> data merit further attention. | We've done that. See our previous <br> comments. |
| In general, the discussion of results could <br> adopt a more critical, analytical <br> perspective to supplement and strengthen <br> the descriptive reporting of the data. <br> Regarding the limitations and reflections, <br> the authors could profitably dig <br> more deeply into some of the variables <br> that might or might not have come <br> into play in generating the results. | Comments from the reviewer are <br> powerfully constructive. Based on <br> these suggestions, we have explored <br> other essentials to complement and <br> strengthen our study findings. In <br> particular, we refine the potential <br> effects that arise as implications of <br> our study findings. This can be <br> found in Paragraphs 5 to 7 in the <br> Discussion section. | 9 |
| 8 | The finding should be related to results <br> from previous literature. The | Regarding the limitations of <br> research and reflection, we discuss <br> it specifically in the last paragraph <br> of the Discussion. |


| conclusion section should highlight the <br> unique contributions of the paper <br> and the limitations of the research. <br> Discussions on what should be done in <br> the future are useful. The discussion and <br> conclusion should make it clear <br> how the research findings contribute to <br> new knowledge. | reviewer. In conclusion, we have <br> highlighted the unique <br> contributions and limitations of our <br> research. <br> We have also provided an <br> explanation regarding what can be <br> done in the future as an implication <br> of our findings, and we briefly <br> highlight it again in the Conclusions <br> section. |
| :--- | :--- | :--- | | In body text: |
| :--- |
| Our research findings are useful for |
| educators in designing mathematics |
| learning that facilitate the development |
| of students' mathematical connections |
| skill. Educators can use our findings to |
| build a framework to rearrange |
| learning objectives, adjust the depth of |
| learning topics, select mathematics |
| contents and contexts, choose |
| innovative strategies, consider the use |
| of technology, even design |
| assessments that consider |
| mathematical connections. We |
| recommend that the topics used to |
| teach mathematics contain problem- |
| solving activities that link several |
| mathematical concepts and procedures |
| and connect mathematics with other |
| disciplines and real-life situations. |
| Regarding the limitations of this study, |
| we suggest that future research |
| investigate the relationship between |
| types of mathematical connection |
| difficulties and the level of student |
| academic performance. Furthermore, |
| the researchers need to conduct |
| investigations related to students' |
| difficulties in making mathematical |
| connections on other topics. We hope |
| that replications can strengthen our |
| research findings. |
| of the paper is required to make it |
| presentable in a research journal. |$\quad 20$

Reviewer 5

| $\#$ | Reviewer's comments | Response | Page <br> No. |
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| 1 | see 10126 | We do not find comments or <br> suggestions from the reviewer in <br> document 10126 |  |
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| Reviewer 6 |  | Response | Page <br> No. |
| :--- | :--- | :--- | :--- |
| $\#$ | Reviewer's comments | it is suggested to check some punctuation <br> marks | We've fixed it. We use Grammarly <br> to solve that. <br> apostrophes or quotation marks in your <br> document. |
| The presentation in the introduction is <br> useful. But has not explained in detail the <br> position of the research, so it is different <br> from previous studies. | We've fixed it. We use Grammarly <br> to solve that. | We have provided a more detailed <br> explanation regarding our study <br> position, which differentiates it <br> from previous studies. Our <br> explanation can be found in <br> Paragraph 9 in the Introduction <br> section. | 4 -5 |
| 3 | In body text: <br> Even though there have been many <br> studies related to mathematical <br> connection, there are still a few studies <br> that are focused on investigating the <br> difficulties experienced by students in <br> making mathematical connections <br> when solving mathematics problems. <br> The study of García-García and Dolores- <br> Flores (2018) is more focused on <br> exploring the types of mathematical <br> connections made by high school <br> students in performing Calculus tasks. <br> Furthermore, the study of Garcia- <br> García and Dolores-Flores (2020) also <br> explores the types of mathematical <br> connections in solving Calculus <br> application problems but involves pre- <br> university. Payton (2019) conducted a <br> study that focuses on interventions <br> that aim to develop mathematical <br> connections. Zengin (2019) tested the <br> use of GeoGebra software for the <br> development of mathematical <br> connections skills. Other studies were <br> conducted to explore mathematical <br> connections involving various <br>  <br> Dolores-Flores, 2018; Mhloo, 2012; <br> Mhlolo et al., 2012; Moon, Brenner, <br> Jacob, \& Okamoto, 2013). Based on this <br> review, we are motivated to explore <br> students' difficulties in making <br> mathematical connections, especially <br> when students interconnect <br> mathematical concepts or procedures <br> when solving mathematics problems. |  |  |


| Also, add urgency to the research you are <br> doing. So this research is considered <br> essential to do. | The urgency of our study can be <br> found in Paragraph 8 in the <br> Introduction section. We have <br> added some relevant references to <br> reinforce our ideas. <br> In body text: <br> The starting point for improvement can <br> be made by identifying students' <br> difficulties in solving mathematics <br> problems (Hadi, Retnawati, Munadi, <br>  <br> Retnawati, 2018; Wijaya, van den <br>  <br> Robitzsch, 2014). In this context, we <br> view that investigating student <br> difficulties when making mathematical <br> connections in solving mathematical <br> problems is urgent. Dolores-Flores et <br> al. (2019) point out that mathematical <br> connections occur when students carry <br> out specific tasks and, therefore, we <br> can identify its processes from the <br> writings or arguments produced by the <br> students. Besides, García-García and <br> Dolores-Flores (2018) argue that <br> students have an important role in <br> reflection for process and learning <br> improvement related to mathematical <br> skill connections. Thus, the findings <br> from the results of identifying what <br> students do in solving mathematics <br> problems that require mathematical <br> connection skills can be used as a <br> reflection to improve mathematics <br> learning. | 4 |
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| Some suggestions related to grammatical, <br> such as sentence hard to read, too many <br> non-content words may indicate <br> wordiness, rewrite the sentence to avoid a <br> dangling modifier. | We really appreciate that <br> suggestion. We've made <br> grammatical improvements <br> considering the suggestions from <br> Grammarly. Here are some <br> examples of the improvements we <br> have made: |  |



| $\|$(Reviewer comment: The <br> subordinate phrase Related to the <br> urgency of the mathematical <br> connection ability does not appear to <br> be modifying the subject this study. <br> Rewrite the sentence to avoid a <br> dangling modifier) |  |
| :--- | :--- | :--- | :--- |
| After: <br> Based on the urgency and the review <br> that has been put forward, this study <br> aims to describe the students' <br> difficulties in making mathematical <br> connections when solving <br> mathematical problems | 5 |


| Reviewer 7 |  |  |  |
| :---: | :---: | :---: | :---: |
| \# | Reviewer's comments | Response | Page No. |
| 1 | The are items in the methodology need to address please the comment section... <br> see 10132 | We do not found the comment(s) in the 10132 document. <br> Although we did not find any specific comments from Reviewer 7, we have improved our study methodology according to the suggestions of other Reviewers. | - |
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| Reviewer 8 |  |  |  |
| :---: | :---: | :---: | :---: |
| \# | Reviewer's comments | Response | Page <br> No. |
| 1 | Paper format, font size, alignment and reference list order should be strongly emphasized. And more guidelines are available on IJLTER Journal website. | We've fixed it according to the editor's instructions. |  |
| 2 | Need to add at least 5 keywords. | We have added two new keywords: mathematics learning; phenomenological study | 1 |
| 3 | Need to discuss more detail for the comparison between the students who had mastered and those who faced difficulties of mathematical connection. | We have added a discussion related to the comparison between students who have mastered and students who have difficulty. This discussion can be found in Paragraph 1 in the Discussion section. | 17 |
| 4 | According to figure 1, the author needs to be detailed that the number of unskilled students is greater than the number of skilled students in every problem. | We've fixed that by displaying the number of students for each category on the chart. See Figure 1. | 9 |
| 5 | Findings and discussions should be presented more detail and visible. | We have improved that, including adding some crucial points on wetting, such as the usefulness of our research (see Paragraph 6 in the Discussion section). We also add a discussion regarding the limitations of our study, their implications for practice, and further research (these can be found in the last paragraph of the Introduction section). | $\begin{gathered} 18 \& \\ 19 \end{gathered}$ |
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| \# | Reviewer's comments | Response | $\begin{aligned} & \hline \text { Page } \\ & \text { No. } \end{aligned}$ |
| 1 | On the result and discussion, discuss the position of student's mastery that you interviewed, give the learning theory that support your solution (problem based learning). | We have added discussions as suggested by Reviewer 7 (position of student's mastery that you interviewed). These discussions can be found in Paragraph 1 in the Discussion section. <br> In body text: <br> The results of this study generally indicate that most students have not mastered the mathematical connection skills well. For each mathematical connection indicator, most students have mastered the different representation indicator (DR) (47.37\%) and the connection where A implies B (IM) (47.37\%) in Problem 2. Whereas in other indicators, the percentage of students the master is still low. Many students have not mastered the mathematical connection indicators for each given mathematical problem, indicating clearly that most students still have difficulty making mathematical connections in solving mathematics problems. Students who have been able to make good mathematical connections show that they have a good understanding of using various mathematical concepts and procedures and their relationships to solve problems. This finding is consistent with the opinion of GarcíaGarcía and Dolores-Flores (2020) and Payton (2019). Conversely, students who have difficulties tend not to master the basic concepts and mathematical procedures needed to solve problems, as stated by students during interviews. Besides, the unfamiliarity of students in solving mathematics problems also causes them to experience difficulties. This unfamiliarity also impacts students' low interest in word problems, where students admit to being lazy to read problems with too long words, as stated by students during interviews. | 17 |


|  | We have also added theory and <br> sharpened the discussion to support <br> the solutions we provide. This can <br> be seen in paragraph 8 in the <br> Discussion section. <br> In body text: <br> We can make various efforts to <br> improve student ability in <br> mathematical connections. As stated <br> by NCTM (2000) that mathematical <br> connection is a tool in problem-solving. <br> This statement means that practicing <br> problem-solving skills in learning <br> mathematics participates indirectly in <br> students' practicing mathematical <br> connection skills. Various studies have <br> reported that some learning models <br> were effectively applied to develop <br> student problem-solving skills such as <br> Problem-Based Learning (PBL) <br> (Kartikasari \& Widjajanti, 2017; <br> Malasari, Nindisari, \& Jaenudin, 2017), <br> collaborative problem-based learning <br> strategy (Widjajanti, 2013) as well as <br> using varied methods in learning such <br> as direct learning, demonstration, <br> practice and exercise, and also using <br> modified instructional media (Jannah, <br> Apriliya, \& Karlimah, 2017). Also, it is <br> crucial to give the students more <br> activities of problem-solving so that <br> they make a habit of it. Students of all <br> ages are more motivated with problem <br> situations that involve them and their <br> classmates (Welchman-Tischler, 1992); <br> use three-dimensional manipulatives <br> (Safi \& Desai, 2017); and use proof <br> approaches (Jiang \& O'Brien, 2012). <br> Another strategy that can be applied is <br> using writing strategies in learning <br> mathematics such as making drawings, <br> pictures, tables, and graphs; providing <br> a clear explanation of problem-solving <br> methods and justifications of <br> processes; and doing a reflection on <br> learning (Haltiwanger \& Simpson, <br> 2013). The use of math software such <br> as GeoGebra has also been <br> recommended to develop students' <br> mathematical connection skills (Zengin, <br> 2019) |
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| Reviewer 10 |  |  |  |
| :---: | :---: | :---: | :---: |
| \# | Reviewer's comments | Response | Page No. |
| 1 | The authors used strong references for their literature resources with over $40 \%$ of their list within the last five years. However, it could have been better if the recent literature sources are improved to about $75 \%$ of them being within the last five years. | We have added several new references to strengthen our theoretical study. For example: <br> Albay, E. M. (2019). <br> English, L. D., Gainsburg, J. (2016). <br> García-García, J., \& Dolores-Flores, C. (2020). <br> Hadi, S., Retnawati, H., Munadi, S., Apino, <br> E., \& Wulandari, N. F. (2018). <br> Osman, S., Yang, C. N. A. C., Abu, M. S., Ismail, <br> N., Jambari, H., \& Kumar, J. A. (2018). <br> Özgen, K. (2016) <br> Palmér, H., \& Van Bommel, J. (2020) <br> Payton, S. (2019). <br> Etc. |  |
| 2 | There was an old reference book (Bogdan R C \& Biklen S K (1982), being too old unless a more recent edition of the same book is considered. There have been alot done for the last 38 years in Qualitative Research worth being cited. I suggest this be reviewed too. | We have replaced the book with the 2007 edition. <br> Bogdan, R. C., \& Biklen, S. K. (2007). Qualitative research for education: An introduction to theory and methods. Boston, MA: Allyn and Bacon. | 7 |
| 3 | The research design and methods were matching the objective of the study. The findings demonstrated that the research achieved expected goals. However, the author(s) felt short of explaining the population size and how the sample size, 31 , was arrived at. If there was some criteria adopted, I believe that could have been boldly covered in the write-up. I suggest that to be included in the review. | These suggestions are the same as those of other reviewers, so we have accommodated these suggestions by providing a more detailed explanation in our research method. | 5-7 |
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# High School Students' Difficulties in Making Mathematical Connections when Solving Problems 

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#### Abstract

The primary purpose of studying mathematics is that students can solve problems, both mathematical and real-life problems. In this way, mathematical connections play an essential role in enabling students to solve mathematical problems. Students' difficulties in mathematical connections can cause difficulties in solving problems. This study aims to describe the mathematical connections difficulties experienced by students when solving mathematical problems. This study is qualitative with a phenomenological approach. Data were collected by using mathematical connection tests and interviews after the test. The participants of this study were 31 high school students from five schools in Yogyakarta Special Region and Central Java Province, Indonesia. Data analysis began with analyzing all students' answers in solving mathematical problems and categorizing the types of difficulties experienced by students. Thematic analysis of the interview data was conducted to reveal the causes of difficulties experienced by students when making mathematical connections. The findings showed that most students experienced difficulties in making mathematical connections, such as in different representations, part-whole relationships, connections between mathematical concepts, and interrelationships between mathematical procedures. Several causes of such difficulties and further actions were also discussed in this study.


Keywords: mathematical connections; mathematical problem-solving; students' difficulties; mathematics learning; phenomenological study

## 1. Introduction

Mathematics is a compulsory subject learned from primary to higher education. This subject plays an essential role in the advancement and development of science and technology, and also contributes directly to human survival. Besides, mathematics is not just arithmetic, but it can also be used to practice a variety of thinking skills, such as critical thinking (Appelbaum, 2000; Lince, 2016; Suh \& Seshaiyer, 2013), creative thinking (Leikin \& Pitta-Pantazi, 2013; Lince, 2016), logical thinking (Hodge, 2003; Lince, 2016), and higher-order thinking skills (Apino \& Retnawati, 2017, 2019). The importance of mathematics encourages many countries to keep creating innovations in strategies and approaches to learning mathematics to make mathematics more understandable and applicable in real-life situations.

One of the keys to learning mathematics is problem-solving (NCTM, 2000; Palmér \& Van Bommel, 2020; Van Zanten \& Van den Heuvel-Panhuizen, 2020). Problemsolving is in line with the spirit of mathematics as a means to develop thinking skills. In the context of mathematics education, this problem solving is used to introduce and familiarize students with how to understand a phenomenon related to mathematical concepts and things associated with the application of mathematics in everyday life (Osman et al., 2018). By using problem-solving, the students are then expected to be able to plan and find solutions to various problems systematically and logically (Albay, 2019). This ability is fundamentally important as it can help the students face increasingly complex challenges in life.

Many kinds of literature categorize problem-solving as one of the competencies that must be possessed for success in the 21st century besides critical thinking, creativity, collaboration, and communication (Albay, 2019; English \& Gainsburg, 2016; Partnership for 21st Century Learning, 2019). Today, problem-solving is no longer seen as a written skill, but from a broader perspective, it evolves into an essential skill used to compete in the world of work and even to answer the challenges of this era. In order to reach this skill, other abilities are needed. As formulated by NCTM (2000), in mathematics learning standards, another ability such as mathematical connection must be practiced by students in addition to problem-solving. NCTM (2000) highlights that the mathematical connection is a tool for problem-solving. Mathematical connections help students recognize and use relationships between mathematical ideas and use them in different contexts (Dolores-Flores, Rivera-López, \& García-García, 2019). Having strong mathematical connections will also enhance mathematical understanding (GarcíaGarcía \& Dolores-Flores, 2018; Kenedi, Helsa, Ariani, Zainil, \& Hendri 2019; Silver, Mesa, Morris, Star, \& Benken, 2009) and student achievement (Kartikasari \& Widjajanti, 2017; Ndiung \& Nendi, 2018). Hence, making mathematical connections is necessary for students to be successful in mathematics education.

Mathematical connections are generally associated with three things, namely connections related to the application of mathematics to real-life contexts (Blum, Galbraith, Henn, \& Niss, 2007; Monroe \& Mikovch, 1994; Mwakapenda, 2008; Özgen 2016), mathematical connections with other disciplines (Blum et al., 2007; Mwakapenda, 2008; Özgen 2016), and connections between mathematical ideas
or concepts themselves (Blum et al., 2007; Eli, Mohr-Schroeder, \& Lee, 2013; Monroe \& Mikovch, 1994; Mwakapenda, 2008). The connection between mathematical ideas or concepts by Businskas (2008) is referred to as interconnections in mathematics, while García-García and Dolores-Flores (2018) mention them as intra-mathematical connections. The ability to make connections between mathematical ideas or concepts themselves (interconnections or intramathematical connections) is crucial for understanding mathematical concepts (Anthony \& Walshaw, 2009; Berry \& Nyman, 2003; García-García \& DoloresFlores, 2020; Mhlolo, 2012) and for their application to other scientific disciplines (Mhlolo, 2012; Mhlolo, Venkat, \& Schäfer, 2012). Thus, interconnection in mathematics becomes an interesting topic to discuss. Businskas (2008) suggests that most literature only focuses on examining the connection between mathematics and real-world situations without exploring how interconnection in mathematics itself. Besides, García-García and Dolores-Flores (2020) reveal that there is still little research focused on investigating the mathematical connection process when students solve mathematics problems. Hence in this study, mathematical connections are focused on interconnection in mathematics itself when students solve mathematical problems.

Businskas (2008) suggests a framework for thinking about mathematical connections in practice. The framework of thinking can be operationally used as an indicator of mathematical interconnections consisting of five categories. The categories include (1) different representation as a form of mathematical connections; (2) part-whole relationships; (3) connections where A implies B; (4) connections showing that $A$ is a procedure for doing $B$; and (5) instructional oriented connection that shows how certain concepts are pre-requisites for understanding related concepts (Businskas, 2008). García-García and DoloresFlores develop a framework similar to Businskas and have implemented it in their research (e.g., García-García \& Dolores-Flores, 2018; 2020). That framework includes several types of mathematical connections indicators, including the following: different representations, procedural features, reversibility, and meaning as a connection. Through these indicators, mathematical connections can be identified more quickly and the extent to which mathematical connections can be easily measured.

Some other studies also report that the students' mathematical connection abilities at various levels need serious attention. Lapp, Nyman, and Berry (2010) report that undergraduate students encountered difficulties in making connections between various concepts, such as the connection between eigenvalues and eigenvectors in algebra learning. Dolores-Flores et al. (2019) explore the mathematical connections of pre-university students when solving tasks involving the rates of change. The result showed that the students only made mathematical connections of procedural types. In contrast, the students scarcely made other types of mathematical connections, such as the common features and the generalization. Siregar and Surya (2017) analyze the junior high school students' abilities in mathematical connections using tests of mathematical connections, and the result showed that their abilities were still low. Similarly, Kenedi et al. (2019) investigate the elementary school students' mathematical connection ability in solving mathematics problems, and the result showed that
their abilities were also low. The results of these studies can be used as a basis for improving the quality of mathematics learning that is oriented towards enhancing mathematical connections.

In practice, several studies report some obstacles in teaching mathematical connections. Dolores-Flores et al. (2019) report that a lack of conceptual understanding and difficulties in manipulating algebra were the main obstacles in making mathematical connections. Arjudin, Sutawidjaja, Irawan, and Sa'dijah (2016) also report that students' difficulties in making mathematical connections were caused by errors in connecting with conceptual knowledge and procedural knowledge. Lack of familiarity with the mathematical connection problems also becomes another obstacle for students in developing their mathematical connection ability. In this way, Agustini, Suryadi, and Jupri (2017) suggest familiarizing students with mathematical connection problems by using openended problems. These findings indicate that actions are needed to improve the quality of mathematics learning, which is oriented towards strengthening mathematical connection skills.

The starting point for improvement can be made by identifying students' difficulties in solving mathematics problems (Hadi, Retnawati, Munadi, Apino, \& Wulandari, 2018; Rafi \& Retnawati, 2018; Wijaya, van den Heuvel-Panhuizen, Doorman, \& Robitzsch, 2014). In this context, we view that investigating student difficulties when making mathematical connections in solving mathematical problems is urgent. Dolores-Flores et al. (2019) point out that mathematical connections occur when students carry out specific tasks and, therefore, we can identify its processes from the writings or arguments produced by the students. Besides, García-García and Dolores-Flores (2018) argue that students have an important role in reflection for process and learning improvement related to mathematical skill connections. Thus, the findings from the results of identifying what students do in solving mathematics problems that require mathematical connection skills can be used as a reflection to improve mathematics learning.

Even though there have been many studies related to mathematical connection, there are still a few studies that are focused on investigating the difficulties experienced by students in making mathematical connections when solving mathematics problems. The study of García-García and Dolores-Flores (2018) is more focused on exploring the types of mathematical connections made by high school students in performing Calculus tasks. Furthermore, the study of GarcíaGarcía and Dolores-Flores (2020) also explores the types of mathematical connections in solving Calculus application problems but involves pre-university. Payton (2019) conducts a study that focuses on interventions that aim to develop mathematical connections. Zengin (2019) examines the use of GeoGebra software for the development of mathematical connections skills. Other studies are conducted to explore mathematical connections involving various representations (e.g., García-García \& Dolores-Flores, 2018; Mhlolo, 2012; Mhlolo et al., 2012; Moon, Brenner, Jacob, \& Okamoto, 2013). Based on this review, we are motivated to explore students' difficulties in making mathematical connections,
especially when students interconnect mathematical concepts or procedures when solving mathematics problems.

Based on the urgency and the review that has been put forward, this study aims to describe the students' difficulties in making mathematical connections when solving mathematical problems. We hope that the findings of this study can provide a framework for educators to improve best practices in mathematics learning, especially related to the development of students' mathematical connection skills.

## 2. Methods

### 2.1. Type of Study

This study was classified as phenomenology, a type of qualitative research methods. The primary aim of phenomenological research was to reduce the experiences of people with a particular phenomenon to find descriptions of the universal essence (Creswell, 2013). The phenomenon in this study was about the students' difficulties in making mathematical connections, especially in solving mathematical problems. One common phenomenon which occurred when students solved mathematical problems was that students already knew a concept, but they had difficulty in connecting the concept with other mathematical concepts. This phenomenon often harms their understanding of mathematical concepts and their academic achievement in learning mathematics.

### 2.2. Participants

The participants of this study were 31 eleventh grade high school students from five schools in Yogyakarta Special Region and Central Java Province, Indonesia. We selected the schools as representatives with high, medium, and low academic achievement. Six students came from school with high academic achievement, 21 students came from school with medium academic achievement, and 12 students came from school with low academic achievement. When we conducted the study, the students involved in this study were between 15 and 17 years old.

### 2.3. Data Collection

We collected data through tests and interviews. The test consisted of mathematical problems (items) containing concepts that had been taught at schools. It comprised of three items, and each of them required a mathematical connection ability to solve it. We took these items from the college entrance exam questions in Indonesia that had been released and re-validated. The validity of the test instrument was proven through content validation by asking experts to agree on the item's suitability with the indicators. The experts were two high school mathematics teachers and two mathematics education lecturers. The indicators of mathematical connection abilities used in this study included different representations (DR), part-whole relationships (PWR), connections where A implies $B$ (IM), and connections showing that $A$ is a procedure for doing $B$ (PD). We used item 1 to measure the students' mathematical connection ability to solve the problem of a two-variable linear equation (see Figure 2). We used item 2 to measure the students' mathematical connection ability to solve the problem of a trigonometric equation (see Figure 3). We used item 3 to measure the students'
mathematical connection ability to solve the problem of a circle (see Figure 4). Before taking the test, we informed students that the test results would not affect their academic achievement in school, but we asked them to take the test seriously. The test was not administered in the regular classroom but taken vacant or available time as agreed by the teacher, students, and researchers in each school. We gave students 30 minutes to complete the test.

We conducted interviews with the students right after they finished the test. The interviews aimed to know the students' perceptions of the problems being tested. In this case, we asked the students to show which difficult parts of the problemsolving process they found. The interviews were also focused on finding obstacles or causes of the difficulties encountered by the students in solving mathematical connection problems. Before the study, we informed the students that the tests and interviews conducted during the data collection would not affect their academic achievement at school. We conducted interviews right after all students have completed the mathematical connection test in each school. Students have interviewed alternately one by one for about 15 minutes. The answers of each student during the interview were noted directly by the researchers.

### 2.4. Data Analysis

Data analysis was preceded by analyzing the answer sheet of each student. Scoring was done by referring to the scoring guidelines prepared by researchers. The scoring guidelines contained solutions and steps for solving (procedures) that students must take when solving problems. In this study, these procedures represent indicators of mathematical connections (see Figure 2 for an example). We gave a score of 1 for each correct procedure performed by students for each mathematical connection indicator, while for the incorrect procedure, we gave a score of 0 .

In Problem 1, there were two procedures of DR, one procedure of IM, and two procedures of PD (see Figure 2). Students were categorized as "High Mastery" if they performed all the procedures correctly for each indicator. If students only performed one correct procedure on the DR and PD indicators, then students were categorized as "Average Mastery". In contrast, if all procedures performed by students did not meet the three mathematical connection indicators, then they were categorized as "Low Mastery".

In Problem 2, there were six procedures of DR, one procedure of IM, and two procedures of PD (see Figure 3). In Problem 2, if students performed at least four correct procedures on the DR indicator, students were categorized as "High Mastery". If students only performed one to three correct procedures, then they were categorized as "Average Mastery", meanwhile if all the procedures performed by students were incorrect, then students were categorized as "Low Mastery". For the IM indicator in Problem 2, the categorization of students was the same as Problem 1.

For Problem 3, there was one procedure of DR, two procedures of PWR, one procedure of IM, and three procedures of PD (see Figure 4). For DR and IM
indicators, students were categorized as "High Mastery" if they could perform the procedure correctly. In contrast, if the procedure was incorrect, then students were categorized as "Low Mastery". For the PWR indicator, students were categorized as "High Mastery" if they performed two procedures correctly, "Average Mastery" if they performed only one procedure correctly, and "Low Mastery" if they performed all procedures incorrectly. As for the PD indicator, students were categorized as "High Mastery" if they performed three procedures correctly, "Average Mastery" if they only performed one to two procedures correctly, and "Low Mastery" if all the procedures were incorrect.

The data obtained were then tabulated based on the students' ability categories (High Mastery, Average Mastery, and Low Mastery) and mathematical connection indicators (DR, PWR, IM, and PD) for each problem. From this tabulation, we obtained the number and percentage of students for each category of ability and mathematical connection indicators for each problem. In this study, we considered students in the Average Mastery and Low Mastery categories as participants who experienced mathematical connection difficulties. Then some of their answers were selected to map the errors made by students for each mathematical connection indicator for each problem. We presented the results of the mapping narratively.

The results of the interviews were qualitatively analyzed using an analytical technique developed by Bogdan and Biklen (2007) by analyzing the relationships between themes from the qualitative data obtained from the interviews. The transcripts of the interview data were then coded independently by two researchers. If there were differences in the coding results, the two researchers together reviewed the data then agreed to determine the correct coding. If there were no differences in coding results, all researchers analyzed the relationship between the coding so that we found the sub-themes. The relationship between the sub-themes was then analyzed so that we found the main themes. We presented the thematic results of the analysis in the table.

This study involved all researchers during the data analysis processes to ensure the validity and reliability in interpreting the qualitative data. All researchers had experienced in the field of qualitative research, especially related to educational issues. Then we discussed the results of the data analysis in a Focus Group Discussion (FGD) involving all researchers and two experts. The two experts were lecturers outside the researchers' institution and had experienced in qualitative research related to educational issues. The FGD discussed research findings and its suitability and consistency with the data obtained from participants.

## Results

3.1. Description of difficulties in students' mathematical connection ability

In this study, we see the students' mathematical connection ability through four primary indicators, namely different representation (DR), part-whole relationships (PWR), connections where A implies B (IM), and connections showing that A is a procedure for doing $\mathrm{B}(\mathrm{PD})$. We categorized the ability of the students to master each of the mathematical connection indicators into three levels
of mastery, including the following: "High Mastery," "Average Mastery," and "Low Mastery". We use the "Average Mastery" and "Low Mastery" levels as a basis for identifying students who experience mathematical connection difficulties. In other words, when the mastery of each indicator only reaches the level of "Average Mastery" and "Low Mastery," the students were then categorized as experiencing mathematical connection difficulties. We present the percentage of students who experience mathematical connections difficulties and the level of student mastery of each indicator in each problem in Table 1.

Table 1. Percentage of students experiencing mathematical connection difficulties

| Indicators of Mathematical Connections | High Mastery |  | Average Mastery |  | Low Mastery |  | Difficulties ${ }^{1)}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $n$ | \% | $n$ | \% | $n$ | \% | $n$ | \% |
| Problem 1: |  |  |  |  |  |  |  |  |
| Different Representation (DR) | 16 | 42.11 | 7 | 18.42 | 15 | 39.47 | 22 | 57.89 |
| Part-Whole Relationships (PWR) | - 2) | - | - | - | - | - | - | - |
| Connections where A Implies B (IM) | 10 | 26.32 | - | - | 28 | 73.68 | 28 | 73.68 |
| Connections that show that A is a procedure for doing B (PD) | 17 | 44.74 | 6 | 15.79 | 15 | 39.47 | 21 | 55.26 |
| Problem 2: |  |  |  |  |  |  |  |  |
| Different Representation (DR) | 18 | 47.37 | 10 | 26.32 | 10 | 26.32 | 20 | 52.63 |
| Part-Whole Relationships (PWR) | - 2) | - | - | - | - | - | - | - |
| Connections where A Implies B (IM) | 18 | 47.37 | - | - | 20 | 52.63 | 20 | 52.63 |
| Connections that show that A is a procedure for doing B (PD) | 10 | 26.32 | 9 | 23.68 | 19 | 50.00 | 28 | 73.68 |
| Problem 3: |  |  |  |  |  |  |  |  |
| Different Representation (DR) | 5 | 13.16 | - | - | 33 | 86.84 | 33 | 86.84 |
| Part-Whole Relationships (PWR) | 1 | 2.63 | 15 | 39.47 | 22 | 57.89 | 37 | 97.37 |
| Connections where A Implies B (IM) | 7 | 18.42 | - | - | 31 | 81.58 | 31 | 81.58 |
| Connections that show that A is a procedure for doing B (PD) | 2 | 5.26 | 13 | 34.21 | 23 | 60.53 | 36 | 94.74 |

Notes:
${ }^{1)}$ Difficulties in mathematical connection are the total number of students who have average and low mastery in each indicator.
${ }^{2)}$ The indicator is not tested in the item.
$n$ is the number of students.

Table 1 shows that the percentage of students who have high mastery in each indicator tested for each question was under $50 \%$. In general, this number shows that most students still experienced difficulty for each indicator of mathematical
connection ability. For Problem 1, Connections, where A Implies the students perceived B (IM) as the most difficult indicator, where $73.68 \%$ of the students experienced difficulty in this indicator. For Problem 2, however, the most difficult indicator perceived by the students was connection showing that A is a procedure for doing B (PD), where $73.68 \%$ of students experienced difficulty in this indicator. For Problem 4, when compared to Problem 1 and Problem 2, the percentage of student difficulties for each indicator of mathematical connection ability was much higher. Of the four mathematical connection indicators tested in Problem 4, more than $80 \%$ of the students had difficulty, and even $97.37 \%$ of the students had difficulty in the part-whole relationships (PWR) indicator. For the PWR indicator, in particular, Problem 1 and Problem 2 have not accommodated this indicator, and therefore, we could not compare the students' difficulty for this indicator in Problem 3. The fact that the PWR indicator reached the highest percentage showed that the students experienced great difficulty in constructing answers using this indicator. Overall, we concluded that the students' mathematical connection difficulties occur in all indicators where PWR is the most difficult indicator, and PD is the second most difficult indicator for the students. The comparison between the students who had mastered and those who faced difficulties in making mathematical connections can be seen in Figure 1.


Figure 1. The comparison between the students who had mastered and those who faced difficulties of a mathematical connection

Figure 1 shows that the gap between students who had mastered the indicators and those who had not mastered the indicators was too big, especially in Problem 3. From Figure 1, we can see that the number of students who have not mastered the indicators is more prominent than those who have mastered the indicators of mathematical connection in each mathematics problem. Meanwhile, the gap for DR, PWR, PD indicators in all problems (Problem 1, Problem 2, and Problem 3) looked different. Thus, we conclude that for each mathematical connection indicator in each given problem, the number of students who experienced difficulty is higher than those who did not experience it.

Qualitative data were also collected to confirm the findings. Based on the results of qualitative data reduction from students' interviews, we present some difficulties faced by the students in solving mathematical connection problems in Table 2.

Table 2. Identification of students' difficulties in making mathematical connections when solving problems

| Identification of Student Difficulty | Conclusion |
| :--- | :--- |
| $\begin{array}{c}\text { The students were unfamiliar with mathematical } \\ \text { connection problems. }\end{array}$ | $\begin{array}{l}\text { The students were not well } \\ \text { The students had difficulty in reading mathematical } \\ \text { trine to solve mathema- } \\ \text { patterns. } \\ \text { Theal connection problems }\end{array}$ |
| Tecause of a lack of fami- |  |
| concepts. |  |
| The students had difficiculty in mathematic manipulation. |  |$]$| The students lacked con- |
| :--- |
| ceptual understanding. |
| The students did not understand several terms in the <br> problems. <br> The students had difficulty in understanding the <br> problems completely. |
| The students found it hard to identify important points <br> from the problems. <br> The students forgot mathematical formulas. |
| The problems included too long words. <br> The problems required repeated reading. |

Based on Table 2, we can understand that there are three main causes of students' difficulties in solving mathematical connection problems. The first is a lack of familiarity with mathematical connection problems, as seen in the following excerpts of student interviews.
"... I've never worked on a problem about fractions like in Problem 1." (Student 3)
"... I've never met a problem about a circle with another circle. A problem with a circle usually asks for tangents only. That's not about a circle intersecting another circle. The problem is difficult and unfamiliar to me." (Student 1)

The student interviews showed that so far, the students were only used to working on routine problems. Thus, they faced difficulty when doing non-routine problems, such as mathematical connection. Besides, they had difficulty in reading mathematical patterns, as expressed by two students in the following interview excerpts.
"... if we can find the pattern, the trigonometric identity is actually easy, but it's difficult for me to find the pattern because I don't have the good sense to do that." (Student 12)
"... I have difficulty seeing the pattern because of its fraction, and in my opinion, solving linear equations in this problem is very difficult." (Student 10)

The difficulty of linking concepts and manipulating mathematical operations caused the students to fail in their attempt to determine the next procedure for solving the problem, as illustrated in the following interview excerpts.

```
"... the problem is not too confusing, but I just don't really understand the
trigonometric identity and quadratic equation, then I find it hard to associate them."
(Student 5)
"... I stopped at A and B because not find the comparison to calculate the value of A
and B." (Student 12)
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Lack of conceptual understanding is one of the causes of the students' difficulty in solving mathematical connection problems, as stated by the students in the following excerpts.
"... I've difficulty in this problem; I don't understand the meaning of 'radius' and also the problem in general. So, I have no idea what the problem means." (Student 2)
"... I'm having a hard time understanding the problem; applying the trigonometric identity is quite difficult for me." (Student 10)
"... I don't understand about calculating the area of a circle, and I find it hard to separate the parts of the circle." (Student 5)

The student interviews proved that the students were still weak in the basic concepts of mathematics. In this case, they did not know the term 'radius' and how to calculate the area of a circle. Their low comprehension of such fundamental concepts caused them to have difficulty in understanding the purpose of the problem. Therefore, they failed to plan the correct procedure for solving the problem.

One of the common challenges faced by the students in problem-solving activities was that they were lazy to read word problems. The following excerpts illustrate this.
"... the word problem consisted of long sentences that demanded a lot of concentration on understanding the points. Well, I can understand the points. So, I separated the points first and then calculated the area." (Student 9)
"... what was asked in the problem was actually quite simple, but the description was not straightforward." (Student 11)

It appeared that the students did not enjoy reading the context or rather long information. This condition led to difficulty in understanding the problem as a whole and also planning mathematical procedures used to solve the problem. As a result, the students' progress in problem-solving related to mathematical connections would be hindered. To illustrate the students' difficulties in making mathematical connections in solving mathematical problems, we will present
examples of cases of student difficulties for each indicator of mathematical connection in the next section.

Table 1 shows that the percentage of students who had difficulty in mathematical connections for each indicator was higher than those who had no difficulty. Although the gap between these two groups varied for the three types of problems given, the percentage of students who had difficulty always dominated those who had no difficulty. In the next section, we will describe some cases regarding the student difficulty in mathematical connections for each indicator.

### 3.2. Different Representation (DR) as a form of a mathematical connection

Of the three problems given to the students, the average percentage of students who experienced difficulty for different representations (DR) indicator was $65.79 \%$. This percentage clearly shows that most students still experienced difficulty in applying this indicator. We present an example of student difficulty in this indicator in Figure 2.


Figure 2. Example of student answer with difficulty in Different Representation (DR)
The example of student answer in Figure 2 shows that this student failed to solve the problem correctly. The failure started when the student made a mistake in designing a mathematical model appropriate to the context of the problem. In step

1 , the student defined two new variables, namely $p$ and $q$, where $p=\frac{1}{A-2 B}$ dan $q=\frac{1}{A+2 B}$. It can be observed that these two variables could not be linked to the two initial equations found in Problem 1. Also, in step 2, it shows that the equation model made was out of sync with the results obtained in stage 1. Based on this finding, it is clear that the student's problem occurred when he was not able to represent the form $\frac{A B}{A^{2}-4 B^{2}}$ Into another form, and therefore incorrectly took another procedure to solve Problem 1.


Figure 3. Another example of student answer with difficulty in Different Representation (DR)

In Figure 3, we present another example of student difficulty in the different representations (DR) indicator. In Figure 3 [a], the error in representing a different form of trigonometric equation occurred in step 4 (inside the box). Likewise, the example of the student's answer in Figure 3 [b], in the red box, it is clear that students incorrectly changed the form $\frac{\cos 2 x}{\sin 2 x}$ into $\tan x$. Meanwhile, in Figure 3 [c], the error began in step 2, which the student manipulated the form of $2 \sin x \cdot \cos 2 x$ and $\cos x \cdot \sin 2 x$ by using the formula for multiplying sine and cosine, and we can see the error in the red box. Examples of these errors provide
empirical evidence that the students still encountered difficulties in the different representations (DR) indicator for solving mathematical connection problems.

### 3.3. Part-Whole Relationships (PWR)

In this study, the PWR indicator for solving mathematical connections problems was only found in Problem 3. The percentage of students who did not master this indicator was the highest among all of the indicators, at $97.37 \%$. This finding strongly indicated that in the context of the given problem, the students' ability to do part-whole relationships was still low. We present examples of student answers that indicate that they have difficulties with the PWR indicator in Figure 4.


Figure 4. Example of the student answer with difficulty in Part-Whole Relationship (PWR) indicator

Figure 4 [a] shows that in step 1, the student actually understood the meaning of Problem 3. However, it appeared that the students had difficulty calculating the segment area of a large circle. Based on the student's answer in Figure 4 [a], the student calculated the area of a large circle segment = the area of a large circle the area of $1 / 2$ small circle. What the student did in this step indicated that he was not able to find the basic concepts used to calculate the area of segment (such as the rules of cosine, the area of the section, and the area of a triangle). In other words, the student encountered difficulty in finding part-whole relationships to find the segment range of the large circle. Next, Figure $4[\mathrm{~b}]$ showed the other example of a student's answer in solving Problem 3. In Figure 4 [b] can be seen that the student found it hard to analyze the parts (see step 1) or the basic concepts used to find the whole solution to Problem 3 (see step 2 and step 3).

### 3.4. Connections where A implies B (IM)

IM indicator in mathematical connections is operationally visible when students can show a relationship that a mathematical concept results in another concept. In the three problems given to the students, each procedure for solving these problems contains an IM indicator. Based on the test of the three problems having the indicator, there were only $30.70 \%$ of the students who mastered the indicator. In contrast, the remaining $69.30 \%$ of the students did not master the indicator. We present the examples of student answers with difficulties in the connections where A implies B (IM) indicator in Figure 5.


Figure 5. Example of student answer with difficulty in Connections Where A Implies B (IM) indicator

From algebra theory, the student's work in Figure 5 [a] was correct, but it was ineffective and required more time to find the final answer. If we compare the student's response in Figure 5 [a] with the solution to Problem 1 (see Figure 2), the difference is evident. The student's work in Figure 5 [a] clearly showed that he/she was not able to simplify the equations given. This finding is because the
student was not able to manipulate the form from $\frac{A B}{A^{2}-4 B^{2}}$ into $\frac{A}{A-2 B} \times \frac{B}{A+2 B}$. As a result, the student failed to find another more straightforward concept (for example, doing mathematical modeling), leading to the discovery of the concept of a two-variable linear equation system. If the student succeeds in finding a more straightforward form of the two-variable linear equation system given, the procedure for solving Problem 1 will be more comfortable.

Meanwhile, as seen in Figure 5 [b], the student made a mistake in step 6. In this step, the student assumed/defined $\tan x=y$, so the trigonometric equation in step 5 could be changed into a quadratic equation $y^{2}+5 y-6=0$. By dividing it into factors (factorizing), the solutions from the quadratic equation were $y=-6$ dan $y=1$ (in Figure $6[b]$, the student wrote the solution as $x_{1}=-6$ and $x_{2}=1$ ). In this case, the solution of the quadratic equation found should be changed into the solution for the trigonometric equation. Because the student previously defined $\tan x=y$, the solution of the quadratic equation is converted into $\tan x=-6$ and $\tan x=1$. Due to some errors in performing the procedure, the final solution for determining the value of $\tan \left(x_{1}+x_{2}\right)$ was also incorrect. From this case, it is clear that the students still had difficulty in connecting a mathematical concept that results in other concepts.

### 3.5. Connections showing that A is a Procedure for Doing B (PD)

Another difficulty experienced by the students in mathematical connections is related to the indicator of connections showing that A is a procedure for doing B (PD). If the students were able to show that a mathematical procedure is applied to obtain another procedure, we consider them competent at this PD indicator. Each of the three problems tested contained the PD indicator, and we obtained the average percentage of the students who experienced difficulties for this indicator was $74.56 \%$. We present the examples of student answers with difficulty in PD indicator in Figure 6.


Figure 6. Example of student answer with difficulty in connections showing that $A$ is a Procedure for Doing B (PD) indicator

In Figure 6 [a], the student was able to find a solution to the trigonometric equation (see step 4 and step 5) resulted from the previous process, even though they did not assume first that $\tan x=x$. However, some errors still occurred in step 7 and step 8 , when the student associated that the value of $x$ is the angle (see step 7). The angles were then substituted with the equation $\tan \left(x_{1}+x_{2}\right)$ (see step 8), even though the intended final solution from Problem 3 was different. This finding clearly showed that the student was not able to connect between the procedures performed in steps 4,5 , and 6 with the equation $\tan \left(x_{1}+x_{2}\right)$ (step 8 ). Likewise, the student's answer in Figure 6 [b], when the student calculated the area of a section (see step 3, inside of the box), they wrote that the section area of the large circle was $\frac{90^{\circ}}{360^{\circ}} \times$ area of a large circle. However, the students did not show what procedure was applied to find a $90^{\circ}$ angle. According to the illustration drawn by the student (see step 1), a $90^{\circ}$ angle was determined based on the assumption that the triangle formed was a right triangle, not associated with cosine rules (see the solution of Problem 3 in Figure 4). This finding showed that the students were not able to show what procedure should be previously applied to calculate the section area of the circle.

## 5. Discussion

The results of this study generally indicate that most students have not mastered the mathematical connection skills well. For each mathematical connection indicator, most students have mastered the different representation indicator (DR) ( $47.37 \%$ ) and the connection where A implies B (IM) ( $47.37 \%$ ) in Problem 2. Whereas in other indicators, the percentage of students the master is still low. Many students have not mastered the mathematical connection indicators for each given mathematical problem, indicating clearly that most students still have difficulty making mathematical connections in solving mathematics problems. Students who have been able to make good mathematical connections show that they have a good understanding of using various mathematical concepts and procedures and their relationships to solve problems. This finding is consistent with the opinion of García-García and Dolores-Flores (2020) and Payton (2019). Conversely, students who have difficulties tend not to master the basic concepts and mathematical procedures needed to solve problems, as stated by students during interviews. Besides, the unfamiliarity of students in solving mathematics problems also causes them to experience difficulties. This unfamiliarity also impacts students' low interest in word problems, where students admit to being lazy to read problems with too long words, as stated by students during interviews.

The results of this study support the findings of several previous studies, which show that the students still experience difficulties in mathematical connection (Dolores-Flores et al., 2019; Kenedi et al., 2019; Lapp et al., 2010; Siregar \& Surya, 2017). Although previous studies involved participants at different levels, from elementary school to undergraduate levels, the obstacles faced by each participant were almost the same in general. Those obstacles consist of difficulty making representations in other forms, doing part-whole relationships, making implications, and showing the interrelationships between mathematical
procedures. These mathematical connection difficulties also occurred in this study.

Of the four mathematical connection indicators studied in this study, most students had difficulty making the part-whole relationship (PWR). This finding is consistent with the findings of Mhlolo (2012) and García-García and DoloresFlores (2020). When doing PWR in solving mathematics problems, students should see the connection between general concepts through specific parts in the form of particular examples (Mhlolo, 2012). In this case, we understand that students are considered capable of making PWR if they apply specific concepts or procedures properly as part of the general concept to be completed. However, in this study, most students failed to do this. To overcome it, according to Mhlolo (2012), students need to be accustomed to doing and expressing generalizations both through deductive and inductive reasoning patterns. When students have good deductive and inductive reasoning skills, we expect that they will be able to do PWR well when solving mathematics problems.

One of the critical factors in making a mathematical connection is a deep understanding of its concept (Dolores-Flores et al., 2019; García-García \& DoloresFlores, 2018; Silver et al., 2009) and obtaining such conceptual understanding also needs mathematical connections (Anthony \& Walshaw, 2009). Dolores-Flores et al. (2019) believed that poor understanding of concepts to be the leading cause of the students' difficulty in making mathematical connections. As also confirmed from the interview conducted in this study, almost all of the students experiencing difficulties in making mathematical connections claimed that they did not understand the mathematical concepts needed to solve mathematical connection problems. For that reason, mathematics learning in the classroom should be focused on how to instill mathematical concepts in students to develop other mathematical skills.

Lack of familiarity with mathematical connection problems also caused difficulties in solving the problems. Mhlolo et al. (2012) suggest that most students lack the opportunity to deepen the understanding of mathematical connections. Besides, the books used have not yet been explicitly linked to the topics with various contexts, mathematics with real-life, and thus hinder the students from developing their mathematical connection skills (Salout et al., 2013). In this case, Baki, Çathoğlu, Coştu, \& Birgin. (2009) recommend the need to make changes in the mathematics class in terms of content and context that must be applied.

The findings of this study have implications for the development of the pedagogy of mathematics learning. We believe that the factors that cause student difficulties in making mathematical connections when solving mathematics problems can be used as a framework for teachers in designing mathematics learning. As stated by García-García and Dolores-Flores (2020), what students do and communicate when solving mathematics problems involving mathematical connections is essential as a reflection to improve the quality of learning. At least the research findings have implications regarding the importance of teachers developing skills
in facilitating students to make mathematical connections and best practices that can be applied to develop students' connection skills.

The teacher's pedagogical competence in training the students to solve mathematical connections also needs immediate attention. It is crucial to ensure that the teacher is well prepared and has confidence that the students have sufficient initial abilities to develop various mathematical skills. Bowen (2014) reports that teachers tend to be hesitant about using their knowledge of mathematical connections because they doubt their student abilities. For this reason, instilling confidence in teachers that their students can develop their ability in mathematical connection is very important. Besides, lack of assistance among the teachers regarding the planning and implementation of learning that facilitates students to make mathematical connections (Monroe \& Mikovch, 1994) is of concern mainly to policymakers in the field of education.

We can make various efforts to improve student ability in mathematical connections. As stated by NCTM (2000) that mathematical connection is a tool in problem-solving. This statement means that practicing problem-solving skills in learning mathematics participates indirectly in students' practicing mathematical connection skills. Various studies have reported that some learning models were effective to develop student problem-solving skills such as Problem-Based Learning (PBL) (Kartikasari \& Widjajanti, 2017; Malasari, Nindisari, \& Jaenudin, 2017), collaborative problem-based learning strategy (Widjajanti, 2013), as well as using varied methods in learning such as direct learning, demonstration, practice and exercise, and also using modified instructional media (Jannah, Apriliya, \& Karlimah, 2017). Also, it is crucial to give the students more activities of problemsolving so that they make a habit of it. Students of all ages are more motivated with problem situations that involve them and their classmates (WelchmanTischler, 1992); use three-dimensional manipulatives (Safi \& Desai, 2017); and use proof approaches (Jiang \& O'Brien, 2012). Another strategy that can be applied is using writing strategies in learning mathematics such as making drawings, pictures, tables, and graphs; providing a clear explanation of problem-solving methods and justifications of processes; and doing a reflection on learning (Haltiwanger \& Simpson, 2013). The use of math software such as GeoGebra has also been recommended to develop students' mathematical connection skills (Zengin, 2019)

Although this study succeeded in uncovering the types of mathematical connection difficulties experienced by students when solving mathematics problems and their causes, this study has not revealed the relationship between students' academic performance levels and difficulties. This limitation provides an opportunity for future research to focus on uncovering the relationship between types of mathematical connection difficulties and the level of student academic performance. Besides, this study's mathematical problems do not represent all mathematics topics studied at the high school level. Thus, to strengthen this study's findings, it is necessary to replicate this study by using mathematical problems on other topics.

## 5. Conclusions and Implications

Based on the study results and discussion, we concluded that the students still experienced difficulties in making mathematical connections when solving mathematics problems. These difficulties included making a different representation as a form of mathematical connections, part-whole relationships (hierarchical nature of concepts), connections that show A is a procedure for doing B (logical reasoning), and connections showing that A is a procedure for doing B (algorithms). In general, the indicators of mathematical connection difficulties experienced by the students as follows. First, lack of familiarity in solving mathematical connection problems characterized by difficulties in recognizing mathematical patterns, linking mathematical concepts, and working out mathematical manipulations. Second, poor understanding of the concept characterized by difficulties in understanding some mathematical terms, comprehending the whole problem, identifying essential points of the problem, applying mathematical formulas. Third, the lack of interest in word problems.

Our research findings are useful for educators in designing mathematics learning that facilitates the development of students' mathematical connections skills. Educators can use our findings to construct a framework to rearrange learning objectives, adjust the depth of learning topics, select mathematics contents and contexts, choose innovative strategies, consider the use of technology, even design assessments that consider mathematical connections. We recommend that the topics used to teach mathematics contain problem-solving activities that link some mathematical concepts and procedures and connect mathematics with other disciplines and real-life situations. Regarding the limitations of this study, we suggest that future research investigate the relationship between types of mathematical connection difficulties and the level of student academic performance. Furthermore, the researchers need to conduct investigations related to students' difficulties in making mathematical connections on other topics. We hope that replications can strengthen our research findings.

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